

One Hundred Years of Cosmology

Einstein, Hawking and the Big Bang

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Midlands Astronomy Club April 2018

Overview



Einstein in 1918



Hawking in 2014

I The theory of relativity

The special theory of relativity

The general theory of relativity

II Relativity and the universe

The static models of Einstein and deSitter

The dynamic models of Friedman and Lemaitre

Hubble's law and the expanding universe

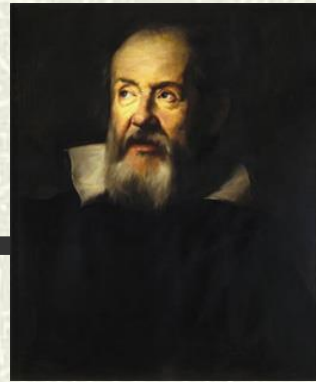
III The big bang model

The question of origins

Hawking-Penrose singularity theorems

Hawking's no-boundary universe

Relativity



Galileo (1564-1642)

■ The principle of relativity

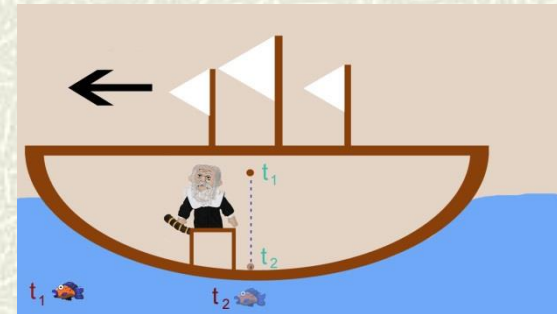
Relativity of motion

Buridan, Oresme, Bruno, Copernicus

■ Galileo's galleon (1632)

Motion of objects in closed cabin of ship

Impossible to detect motion of ship by experiments in cabin

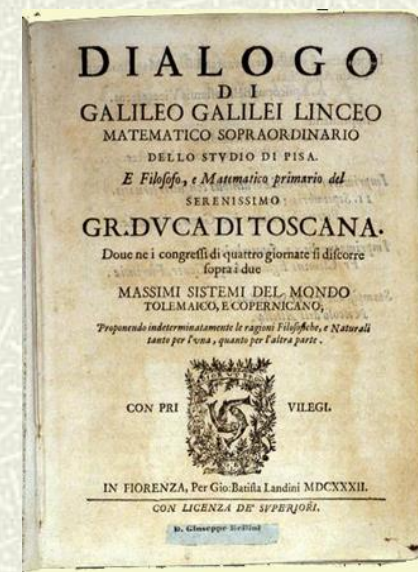


■ Implications for cosmology

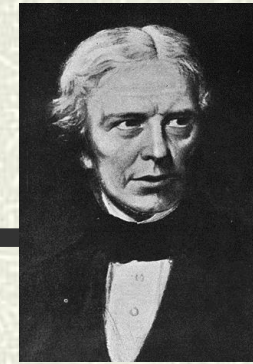
Motion of earth undetectable to passengers

■ Implications for mechanics

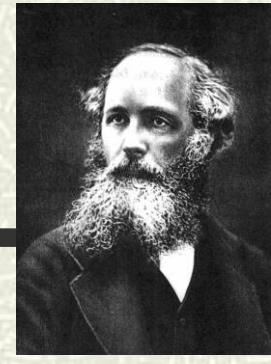
Anticipates Newton's law of inertia



Relativity in the 19th century



Michael Faraday



JC Maxwell

⌘ Electromagnetism

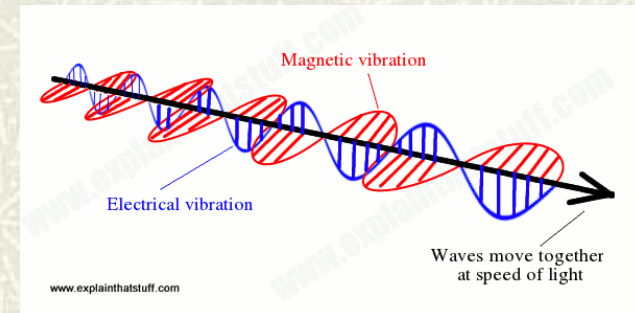
Electricity and magnetism = electromagnetism

Speed of electromagnetic wave = speed of light in vac

⌘ Light = an electromagnetic wave

Changing electric and magnetic fields

The electromagnetic spectrum

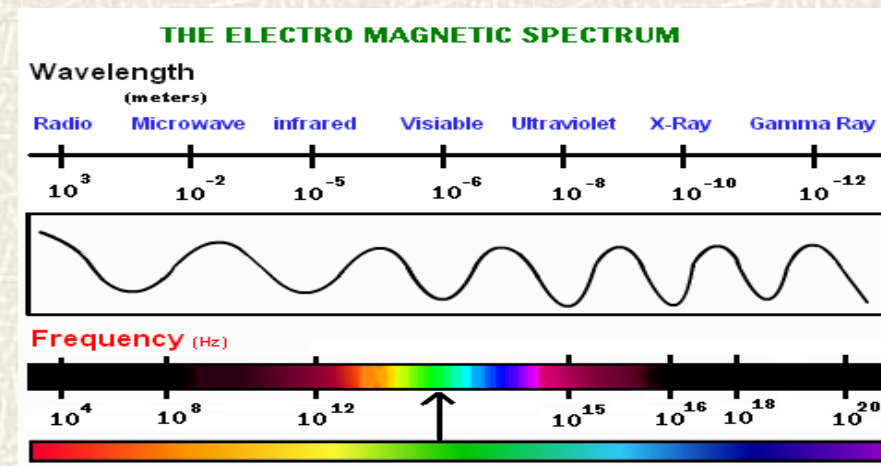


⌘ Speed relative to what?

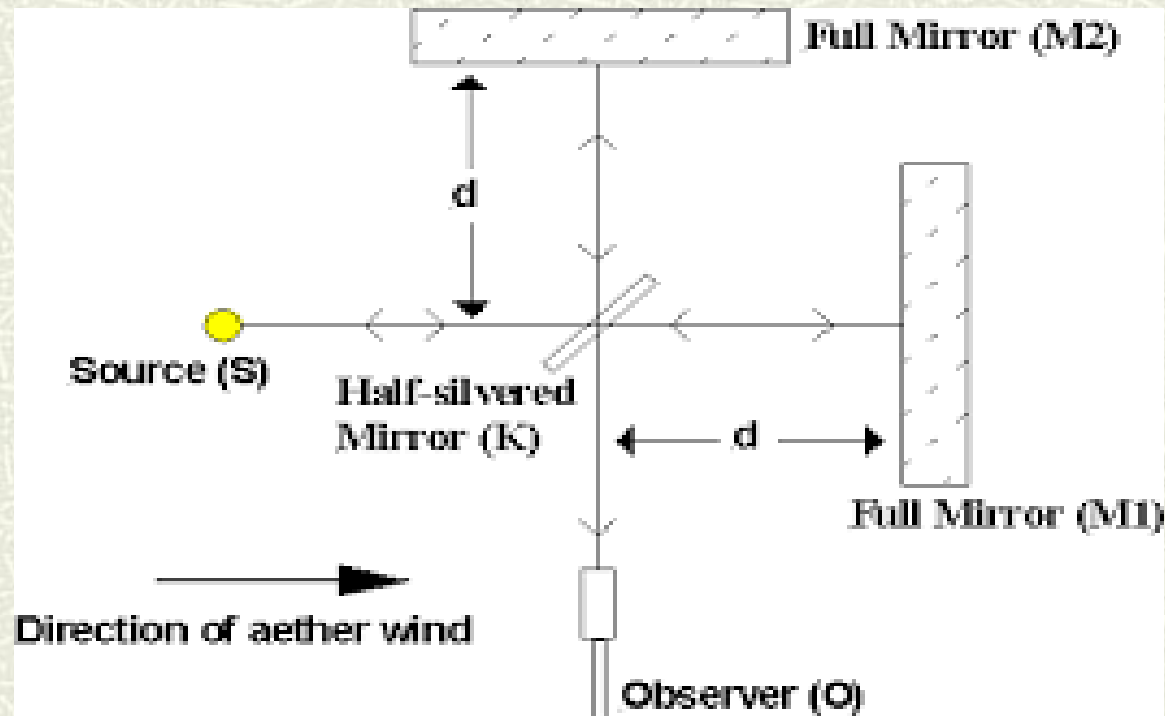
The concept of the ether

⌘ The search for the ether

Michelson-Morley experiment



Michelson-Morley experiment



Expect: rays should arrive at O out of phase

Result: no effect detected

The special theory of relativity (1905)

■ Two principles

*Laws of **all** physics identical for observers in relative uniform motion*

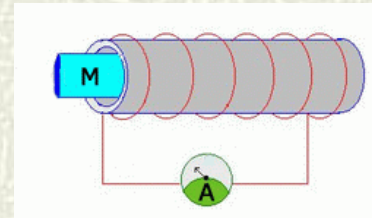
Speed of light in vacuum a universal constant



■ Implications

Intervals in distance and time not universal

Experienced differently by bodies in relative uniform motion



■ Predictions (high-speed bodies)

Length contraction : time dilation

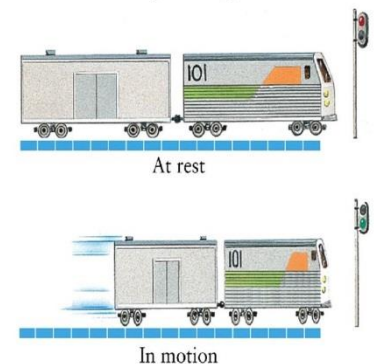
Mass increase; mass-energy equivalence

■ Minkowski space-time (1908)

Space-time invariant for observers in relative uniform motion

$$ds^2 = dx^2 + dy^2 + dz^2 - c^2 dt^2$$

Special Relativity: Length Contraction

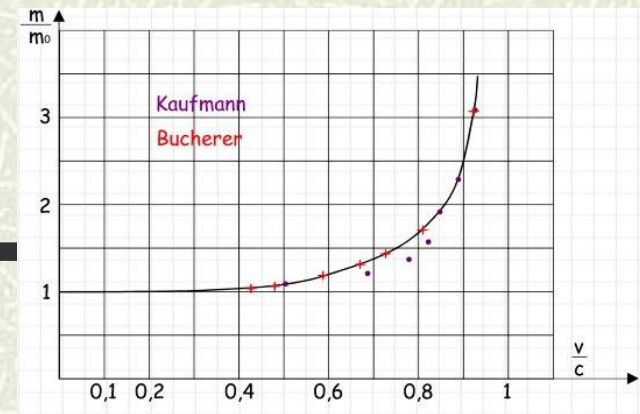


Evidence for SR

Mass increase

The experiments of Kaufmann and Bucherer

$$m' = \frac{m_0}{\sqrt{1 - v^2/c^2}}$$

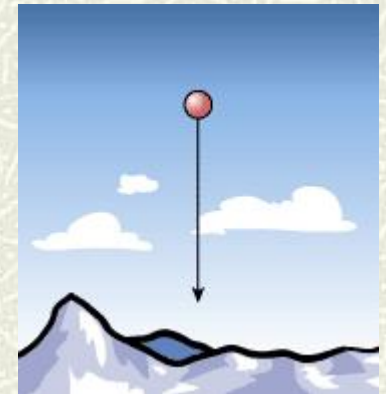


Time dilation

The long-lived muon

$2 \mu s \rightarrow 22 \mu s$

$$t' = \frac{t_0}{\sqrt{1 - v^2/c^2}}$$



Invariance of the speed of light

Always measured as c

Particle experiments at the LHC

Maximum velocity = c

Mass increase

Particle creation

$$E = mc^2$$



The general theory of relativity (1916)

✚ Extending the special theory (1907-)

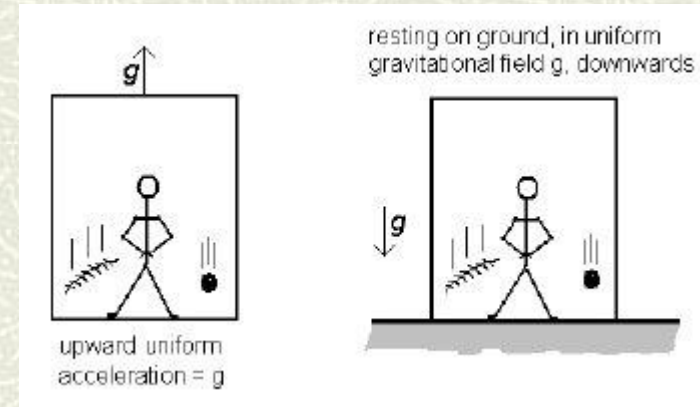
Relativity and accelerated motion?

Relativity and gravity?

✚ The principle of equivalence

Equivalence of gravity and acceleration

Extension of Galileo's principle



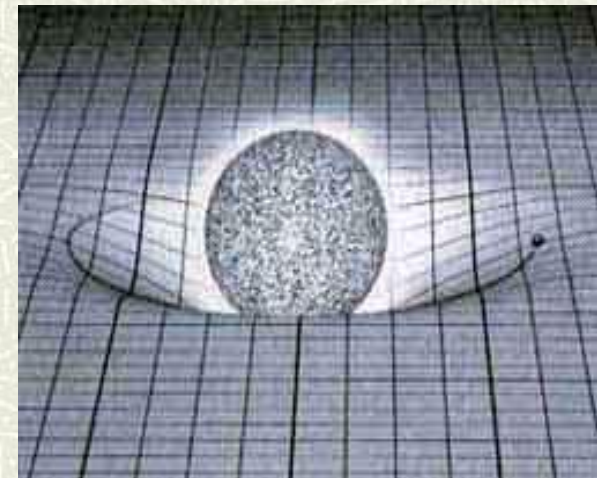
✚ The principle of Mach

Inertial mass defined relative to matter

✚ A long road (1907-1915)

Space-time determined by matter

Gravity = curvature of space-time



The field equations of GR (1915)



$$G_{\mu\nu} = - \frac{8\pi G}{c^4} T_{\mu\nu}$$



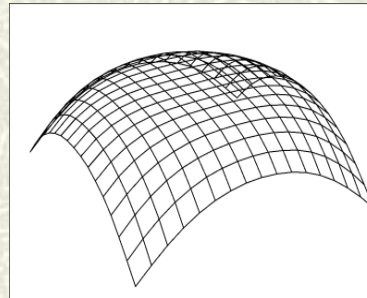
10 non-linear differential equations that relate the geometry of space-time to the density and flow of mass-energy

SR

$$ds^2 = dx^2 + dy^2 + dz^2 - c^2 dt^2$$

$$ds^2 = \sum_{\mu, \nu=1}^4 n_{\mu\nu} dx^\mu dx^\nu$$

$$n_{\mu\nu} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$



GR

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu$$

$$ds^2 = \sum_{\mu, \nu=1}^4 g_{\mu\nu} dx^\mu dx^\nu$$

$g_{\mu\nu}$: variables determined by matter

Evidence for GR

✚ Bending of distant light by stars

Gravitational lensing

✚ Gravitational redshift

Shift in wavelength of light due to gravity

✚ Gravitational time dilation

GPS corrections

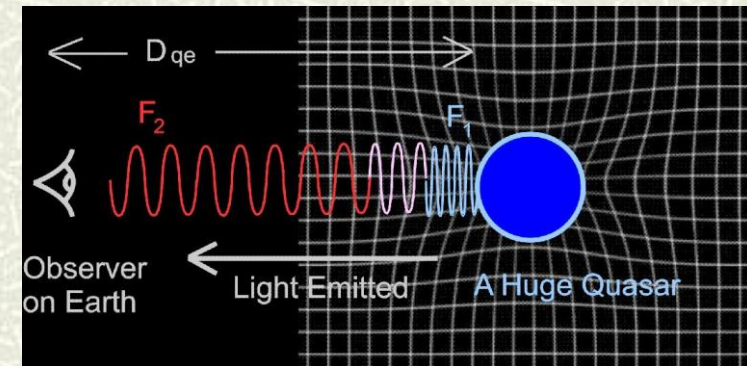
✚ Black holes

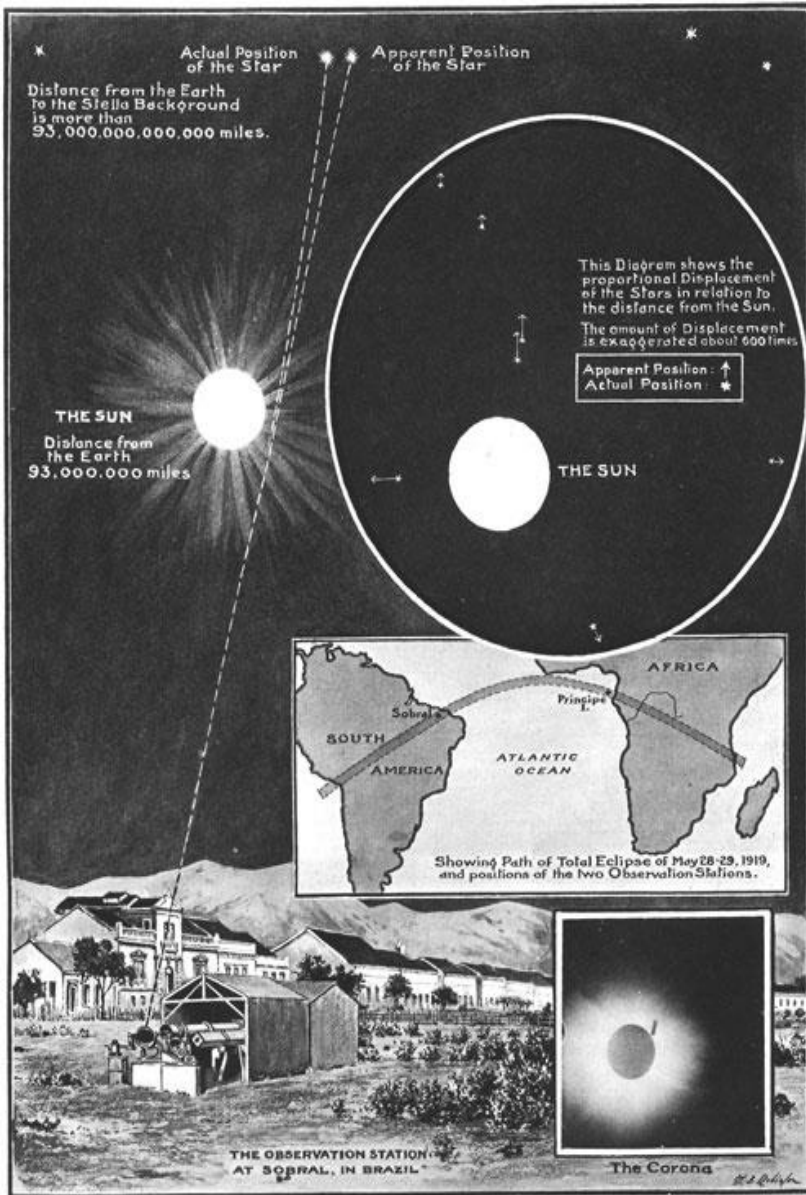
Centre of galaxies

✚ Gravitational waves

Hulse –Taylor binary system

BH, neutron-star mergers





Eclipse Results (1919)

Sobral: $1.98'' \pm 0.16$

Principe: $1.7'' \pm 0.4$

Einstein famous (1919)

LIGHTS ALL ASKEW IN THE HEAVENS

Men of Science More or Less
Agog Over Results of Eclipse
Observations.

EINSTEIN THEORY TRIUMPHS

Stars Not Where They Seemed
or Were Calculated to be,
but Nobody Need Worry.

A BOOK FOR 12 WISE MEN

No More in All the World Could
Comprehend It, Said Einstein When
His Daring Publishers Accepted It.

Asymmetric controversy (Collins and Pinch 1970s)

Claim of bias; rebutted by astronomers (RAS)

Relativity and the universe

Einstein: apply GR to the Universe (1917)

Ultimate test for new theory of gravitation

Assumptions

Uniform, static distribution of matter

Mach's principle: metric tensor to vanish at infinity

Boundary problem!

Assume cosmos of closed curvature

Snag...no consistent solution from GFE

New term needed in field equations!

Cosmic constant – allowed by theory

Anti-gravity effect?

Radius and density defined by λ

Doc. 43

Cosmological Considerations in the General Theory of Relativity

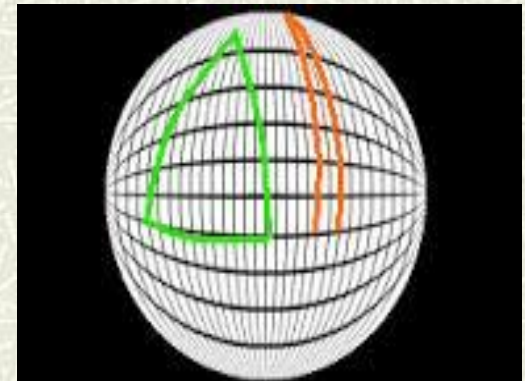
This translation by W. Perrett and G. B. Jeffery is reprinted from H. A. Lorentz et al., *The Principle of Relativity* (Dover, 1952), pp. 175–188.

It is well known that Poisson's equation

$$\nabla^2 \phi = 4\pi K \rho \quad (1)$$
 in combination with the equations of motion of a material point is not as yet a perfect substitute for Newton's theory of action at a distance. There is still to be taken into account the condition that at spatial infinity the potential ϕ tends

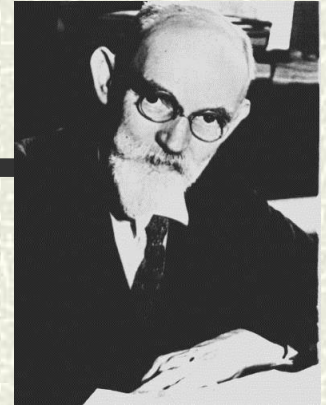
$$G_{\mu\nu} = -\kappa T_{\mu\nu}$$

$$G_{\mu\nu} + \lambda g_{\mu\nu} = -\kappa T_{\mu\nu}$$



$$\lambda = \frac{\kappa \rho}{2} = \frac{1}{R^2}$$

De Sitter's universe



Alternative cosmic solution for the GFE

A universe empty of matter (1917)

Solution B

Cosmic constant proportional to curvature of space

$$\lambda = 3/R$$

Disliked by Einstein

Conflict with Mach's principle

Problems with singularities? (1918)

The de Sitter confusion

Static or non-static - a matter of co-ordinates?

Weyl, Lanczos, Klein, Lemaître

[p. 270] 5. "Critical Comment on a Solution of the Gravitational Field Equations Given by Mr. De Sitter"

[Einstein 1918c]

SUBMITTED 7 March 1918

PUBLISHED 21 March 1918

IN: *Königlich Preußische Akademie der Wissenschaften (Berlin). Sitzungsberichte* (1918): 270–272.

[1] Herr De Sitter, to whom we owe deeply probing investigations into the field of the general theory of relativity, has recently given a solution for the equations of gravitation¹ which, in his opinion, could possibly represent the metric structure of the universe. However, it appears to me that one can raise a grave argument against the admissibility of this solution, which shall be presented in the following.

The De Sitter solution of the field equations

$$G_{\mu\nu} - \lambda g_{\mu\nu} = -\kappa T_{\mu\nu} + \frac{1}{2}g_{\mu\nu}\kappa T \quad (1)$$

is

Prediction of redshifts – astronomical interest

The motion of the nebulae

The redshift of the nebulae

V.M Slipher (Lowell Observatory)

Light from most nebulae redshifted (1915, 1917)



Vesto Slipher

Doppler effect

*Frequency of light depends on
motion of source relative to observer*

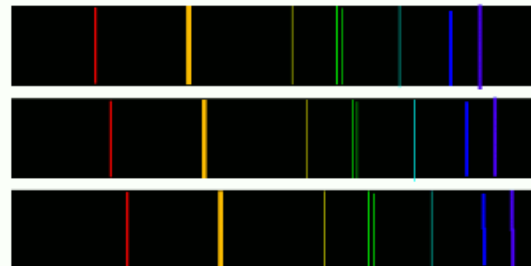
Nebulae moving outward?

Galaxies moving outward?

red shift

no motion

blue shift



Lowell Observatory

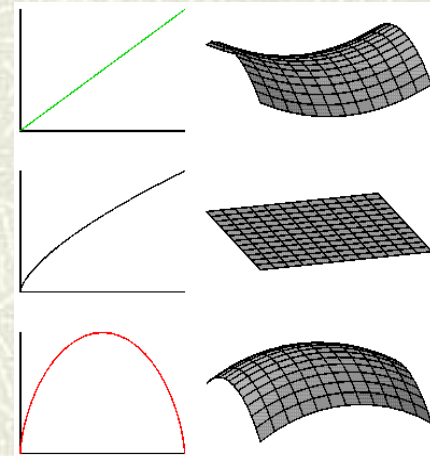
The dynamic universe (theory)



Alexander Friedman (1922)

Allow time-varying solutions for the cosmos

Two differential equations for R



Evolving universe

Time-varying radius and density of matter

Considered 'suspicious' by Einstein

Georges Lemaître (1927)

Theoretical universe of time-varying radius

Expanding universe in agreement with emerging astronomical data

Also rejected by Einstein



“Vôtre physique est abominable”

Astronomy and the universe



Hubble's law (1929)

A redshift/distance relation for the galaxies

Linear relation: $h = 500 \text{ kms}^{-1} \text{Mpc}^{-1}$

Edwin Hubble (1889-1953)

Evidence of cosmic expansion?

RAS meeting (1930): Eddington, de Sitter

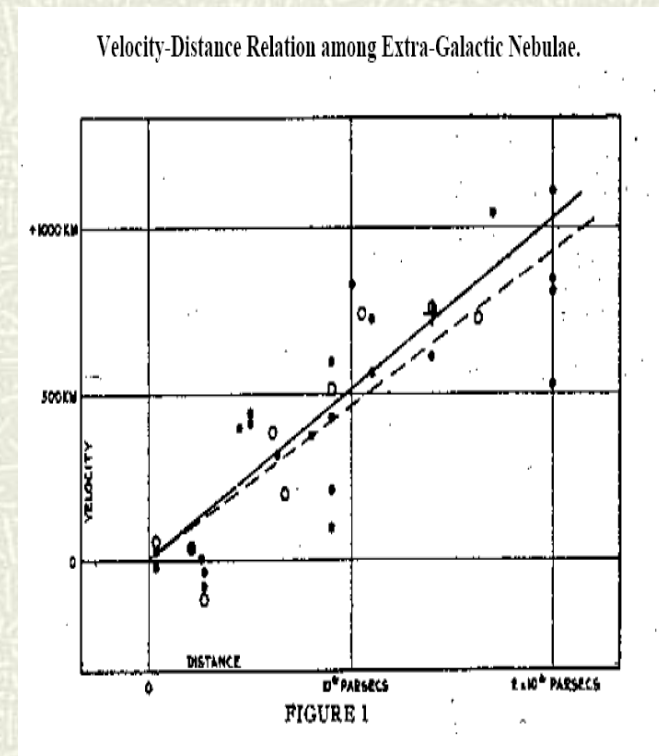
Friedman-Lemaître models circulated

Time-varying radius and density of matter

Einstein apprised

Sojourn at Cambridge (June 1930)

Sojourn at Caltech (Spring 1931)



The expanding universe (1930 -)

- **Eddington (1930, 31)**

On the instability of the Einstein universe
Expansion caused by condensation?

- **Tolman (1930, 31)**

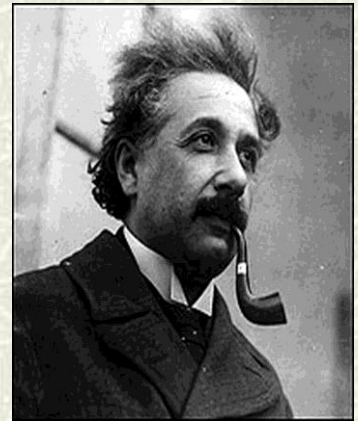
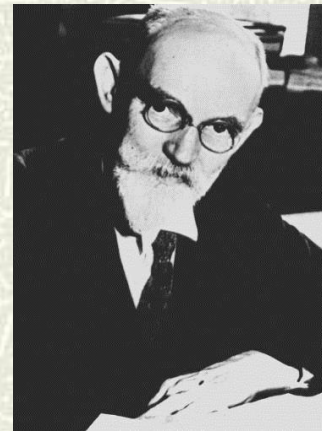
On the behaviour of non-static models
Expansion caused by annihilation of matter ?

- **de Sitter (1930, 31)**

Further remarks on the expanding universe
Expanding universes of every flavour

- **Einstein (1931, 32)**

Friedman-Einstein model $k=1, \lambda=0$
Einstein-de Sitter model $k=0, \lambda=0$



Expanding models
No mention of origins

Cosmic prediction: the big bang



Fr Georges Lemaître

- # **Lemaître 1931:** expanding U smaller in the past
- # Extrapolate to very early epochs
- # Extremely dense, extremely hot
- # Expanding and cooling ever since
- # ‘Fireworks beginning’ at $R = 0$?



Not endorsed by community (1930-60)

Singularity problem: timescale problem

Later called **‘The big bang’**

A second line of evidence

Gamow and nuclear physics (1940s)

Student of Friedman

How were the chemical elements formed?

Problems with stellar nucleosynthesis

Elements formed in the infant hot universe?

Theory predicts $U = 75\%$ Hydrogen, 25% Helium

Agreement with observation

Support for big bang model?



Georges Gamow



Heavier atoms formed in stars

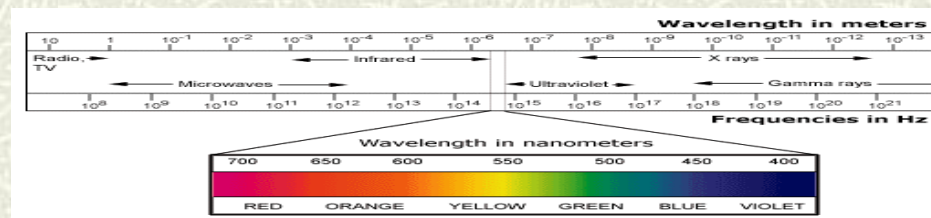
Bonus: a third prediction

- # Infant universe very hot
- # Dominated by radiation
- # Radiation still observable today?
Low temp, microwave frequency
- # A fossil from the early universe!
Released when atoms formed (300,000 yr)

No-one looked



Alpher, Gamow and Herman



The steady-state universe (1948)

‡ Expanding but unchanging universe

Hoyle, Bondi and Gold (1948)

Disliked extrapolation to early epochs

Perfect cosmological principle?

‡ Requires continuous creation of matter

Very little matter required

No beginning, no age paradox

‡ Replace λ with creation term (Hoyle)

$$G_{\mu\nu} + C_{\mu\nu} = -k T_{\mu\nu}$$

‡ Improved version (1962)

$$G_{\mu\nu} + \lambda g_{\mu\nu} = k T (C_{\mu} + C_{\nu})$$



Bondi, Gold and Hoyle



Hoyle and Narlikar (1962)

Steady-state vs big bang (1950-70)

Optical astronomy (1950s)

Revised distances to the nebulae (Baade, Sandage)

New timescale of expansion



Allen Sandage

Radio-astronomy (1960s)

Galaxy distributions at different epochs

Cambridge 3C Survey (Ryle)

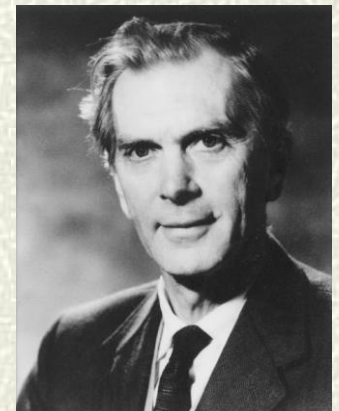
Nucleosynthesis of light elements

Gamow et al. 1948

Cosmic microwave background (1965)

Low temperature, low frequency

Remnant of young, hot universe



Martin Ryle

Cosmic background radiation (1965)

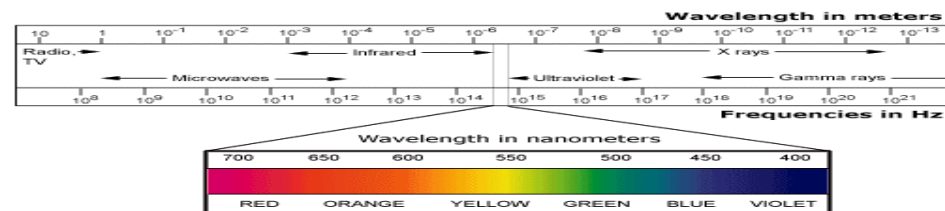
CMB discovered accidentally

- ▣ Ubiquitous signal
- ▣ Low frequency (microwave)
- ▣ Low temperature (3K)



Penzias and Wilson (1965)

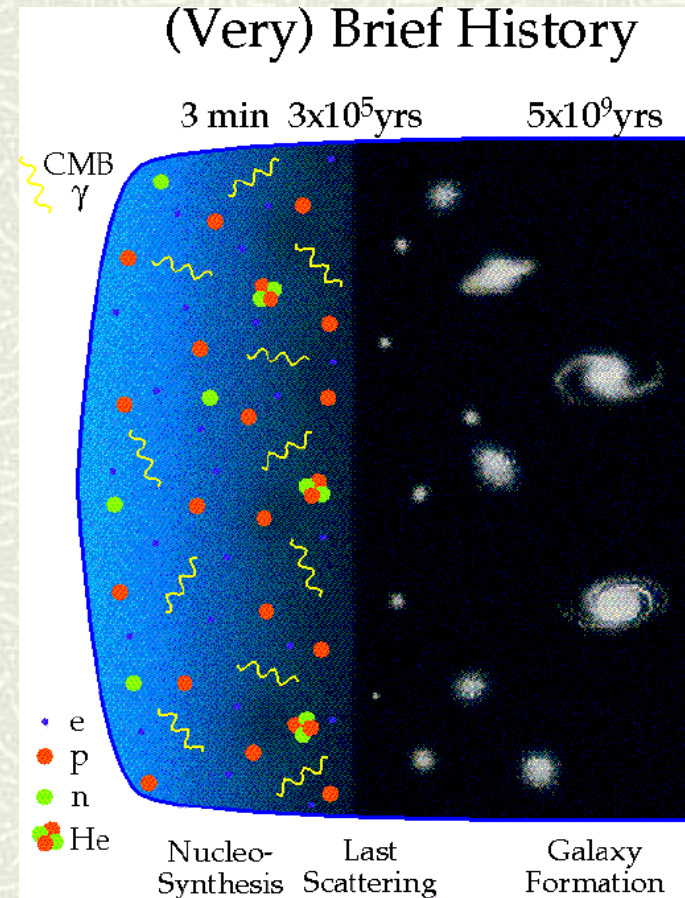
*Echo of **Big Bang!***



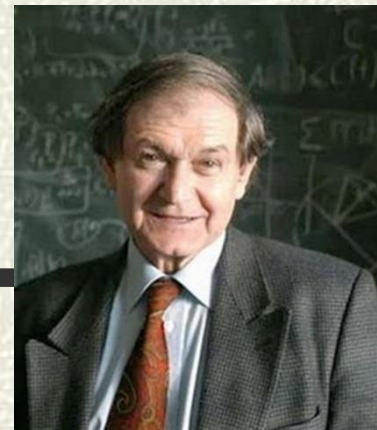
The big bang – evidence

1. The expansion of the U
2. The abundance of H and He
3. The distribution of the galaxies
4. The cosmic microwave background

How did it start?



Problems : theory



⌘ The singularity problem revisited

A facet of simplified assumptions?

⌘ Roger Penrose: black holes

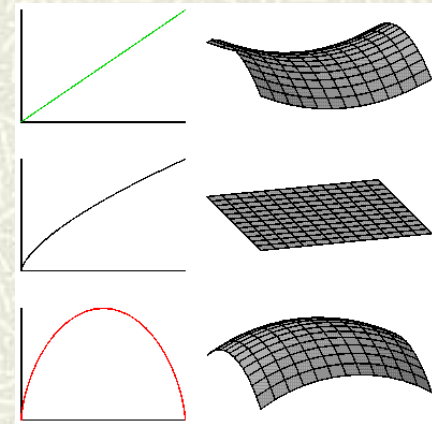
GR \rightarrow BH must contain spacetime singularity

⌘ Stephen Hawking: cosmology

GR \rightarrow U must begin in a spacetime singularity

⌘ Grand cosmological theorem (Hawking/Penrose)

“There is a singularity in our past” (PhD, 1966)

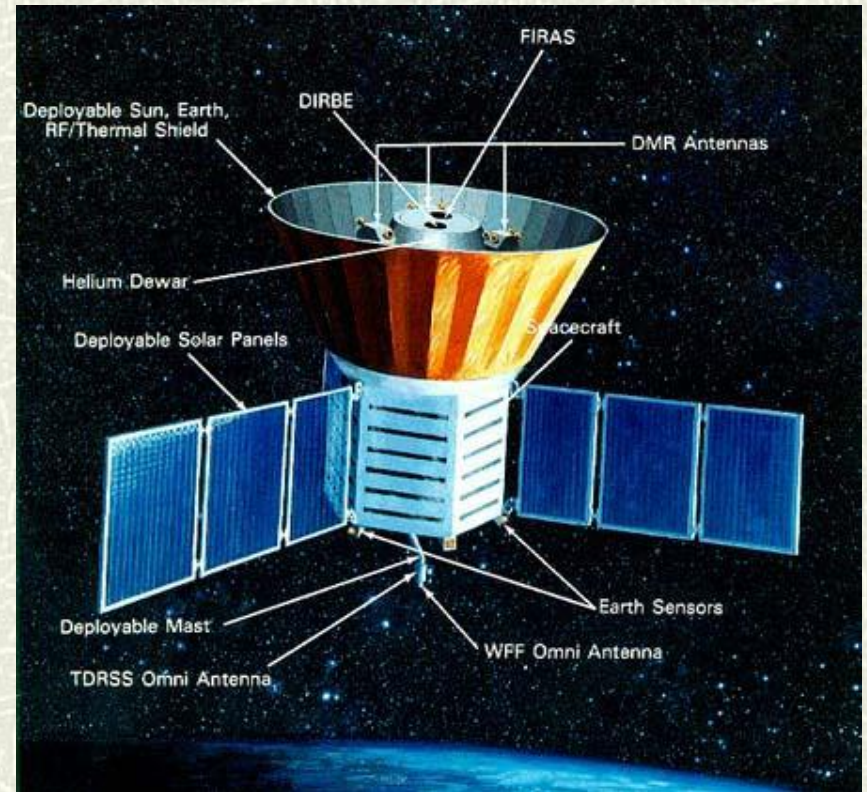


Big bang not a full theory?



Modern measurements of the CMB

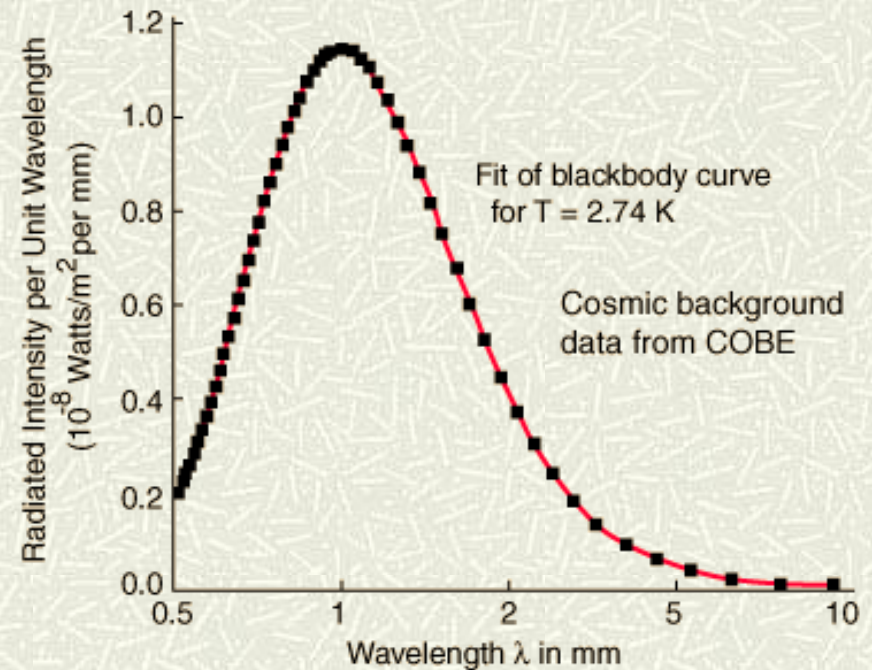
- Details of background radiation
 - Full spectrum
 - Comparison with theory
 - Perturbations?
-
- *Ground telescopes*
 - *Balloon experiments*
 - *Satellite experiments*



COBE satellite (1992)

COBE measurements of CMB

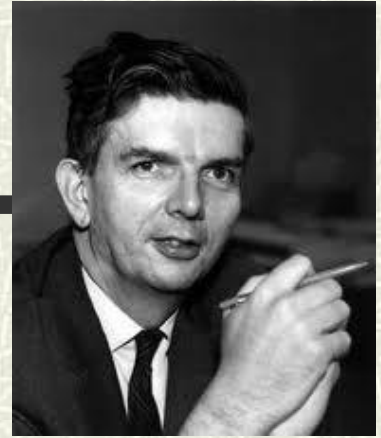
- Expected temperature
- Expected frequency
- Perfect blackbody spectrum
- *Radiation very uniform*
- *Variation of 1 in 10^5*
- *Seeds of galaxies ?*



Nobel Prize

COBE (1992)

Problems: observation



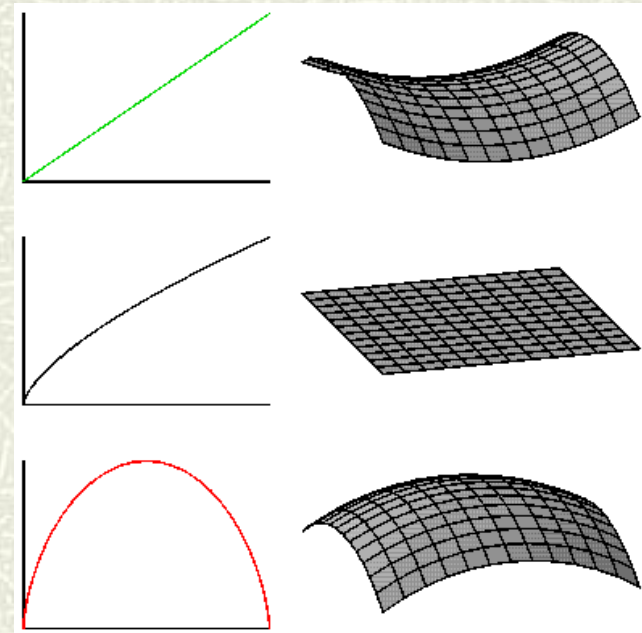
Robert Dicke

Background radiation raised new questions

- ✦ Horizon problem *why so uniform?*
- ✦ Galaxy problem *how did galaxies form?*
- ✦ Flatness problem *fine balance?*

Conflict between theory and experiment

Astrophysics: $\Omega = 0.3$ (incl. DM)

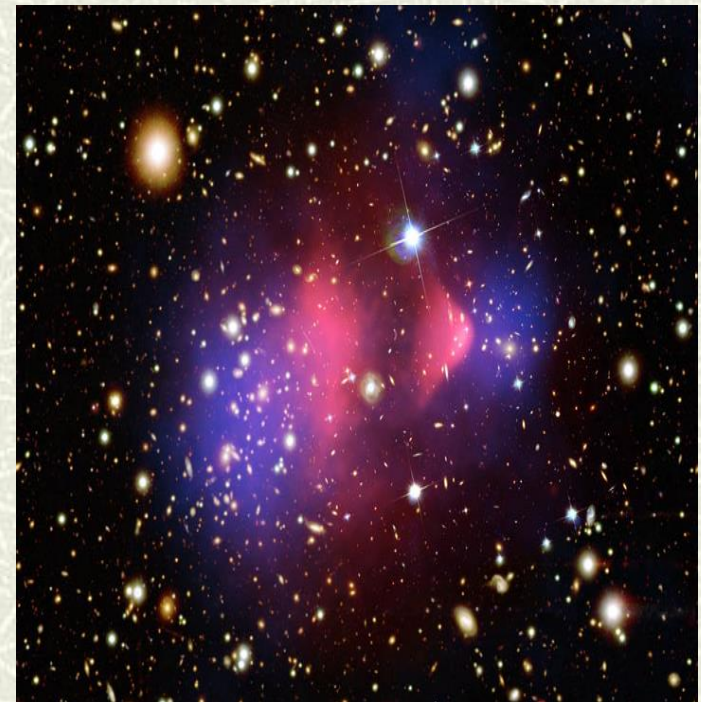


Dark Matter

- ✦ First suggested in 1930s
- ✦ Stellar motion

*normal gravitational effect but
cannot be seen directly*

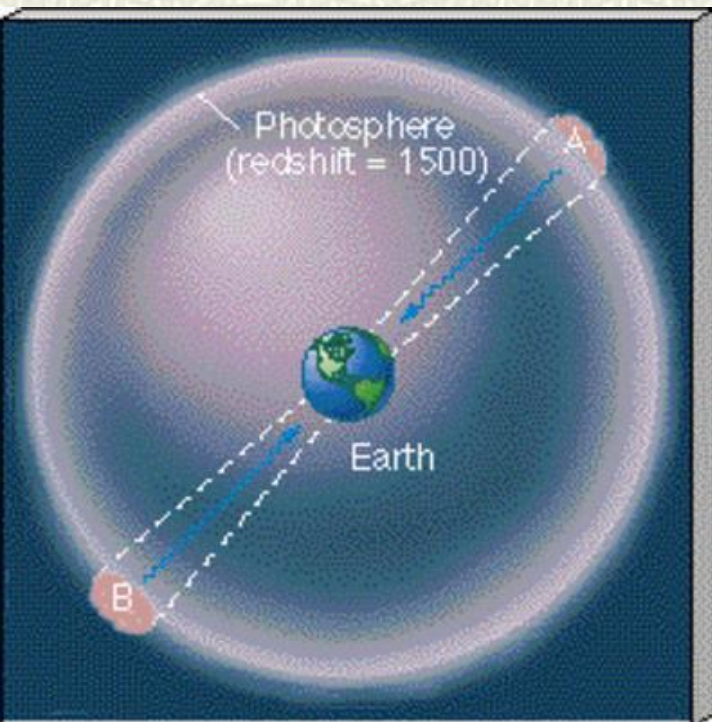
- ✦ Explains motion of stars
- ✦ Explains motion of galaxies
- ✦ Explains gravitational lensing



Matter = OM (20%) + DM (80%)

$\Omega = 0.3$?

The horizon problem



- Two distant regions of microwave background have similar temps

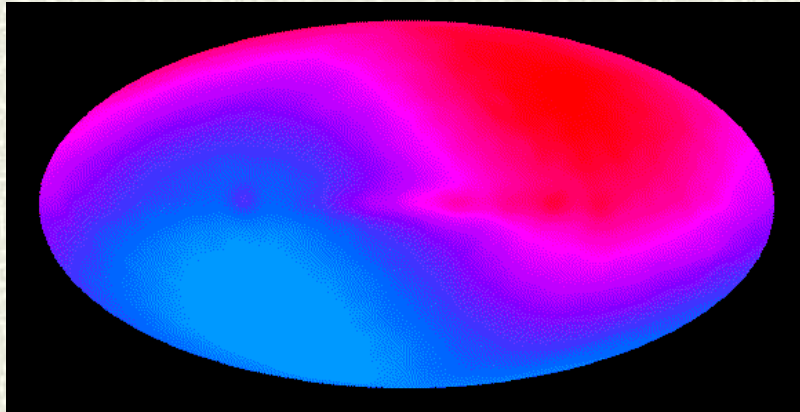
Why?

Too far apart to be causally connected

- Finite speed of light
- Finite age of cosmos

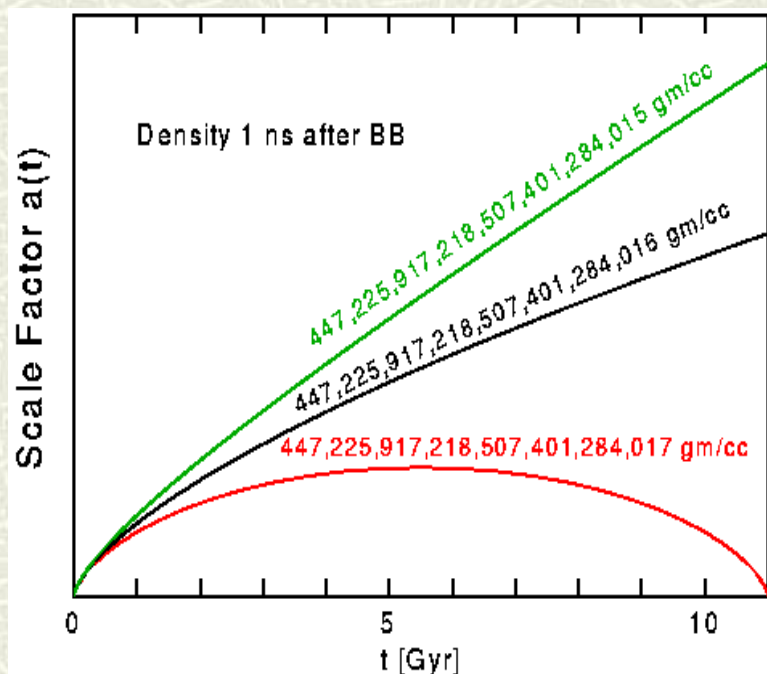
Something wrong with lookback

Galaxy formation problem



- ✦ Microwave background smooth on large scale
- ✦ No deviations from homogeneity obvious
(1 in 10,000)
- ✦ How did slight perturbations become galaxies?

The flatness problem



At $t = 1 \text{ s}$, $\Omega = 1$ to within $1:10^{15}$)

Slightest deviation from flatness



runaway expansion or crunch

Not observed

Why so finely balanced initially?

$$\Omega = 1?$$

Astrophysics: $\Omega = 0.3$?

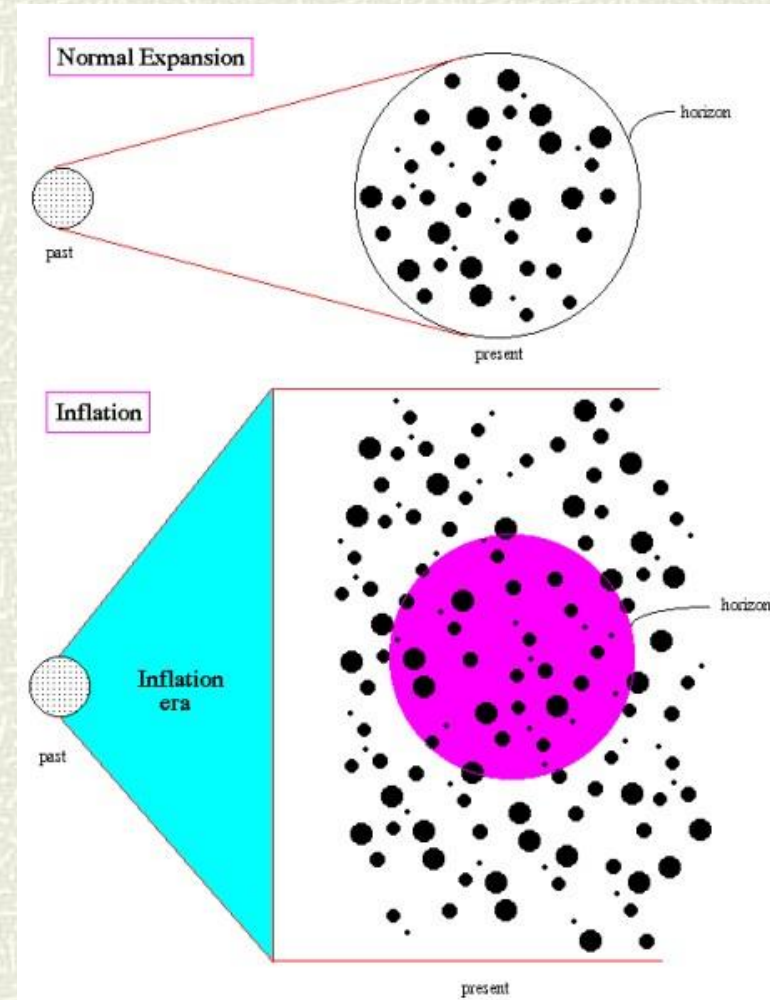
The Theory of Inflation (1981)

- Initial **exponential expansion**
- Driven by *phase transition*

Repulsive force

- Expansion of 10^{35} in 10^{-32} s
- Smooths out inhomogeneities
- Smooths out curvature

'No hair' universe

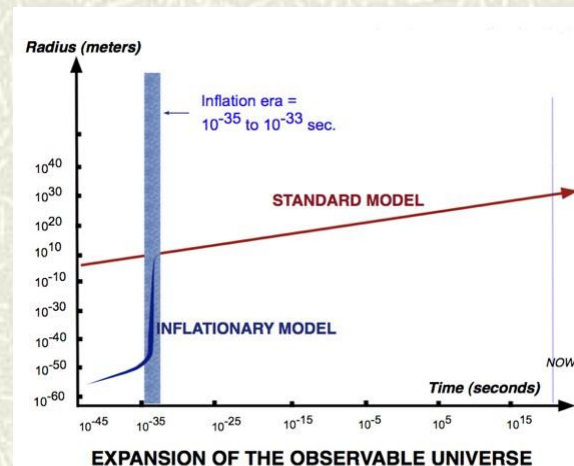
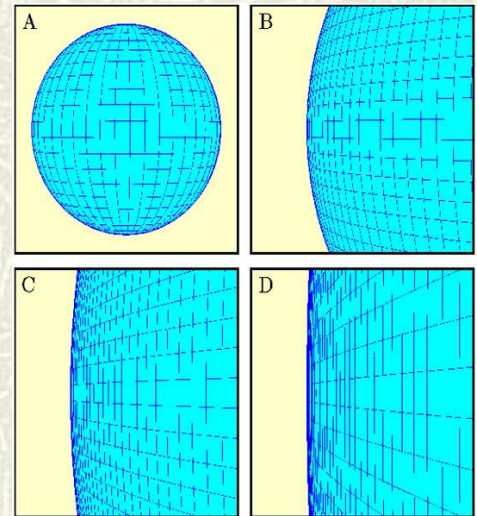


The inflationary universe (1981)

- ⌘ Solves horizon problem
Early U incredibly small
- ⌘ Solves flatness problem
Geometry driven towards flatness
- ⌘ Mechanism for galaxy formation
1982 Nuffield workshop (Hawking)
Quantum fluctuations inflated
Correct spectrum

$$\Omega = 1 ?$$

Conflict between theorists and experimentalists



The accelerating universe (1998)

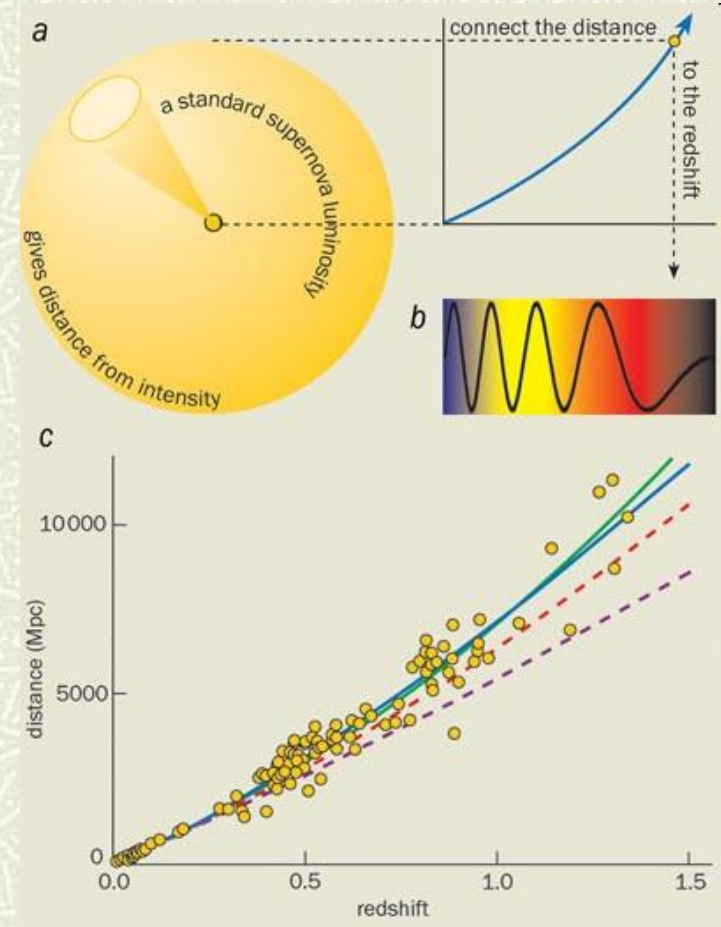
- Supernovae as standard candles (1998)

- Furthest galaxies too far away

- Expansion accelerating

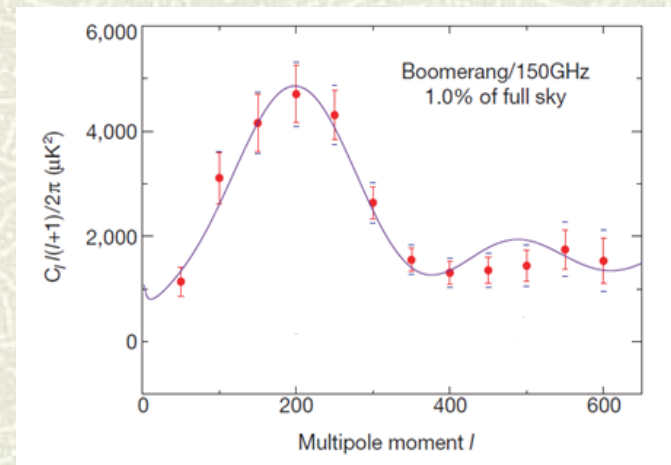
- Implies repulsive energy
Dark Energy ($\lambda \neq 0$)

- Possible support for inflation ($\Omega = 1$?)



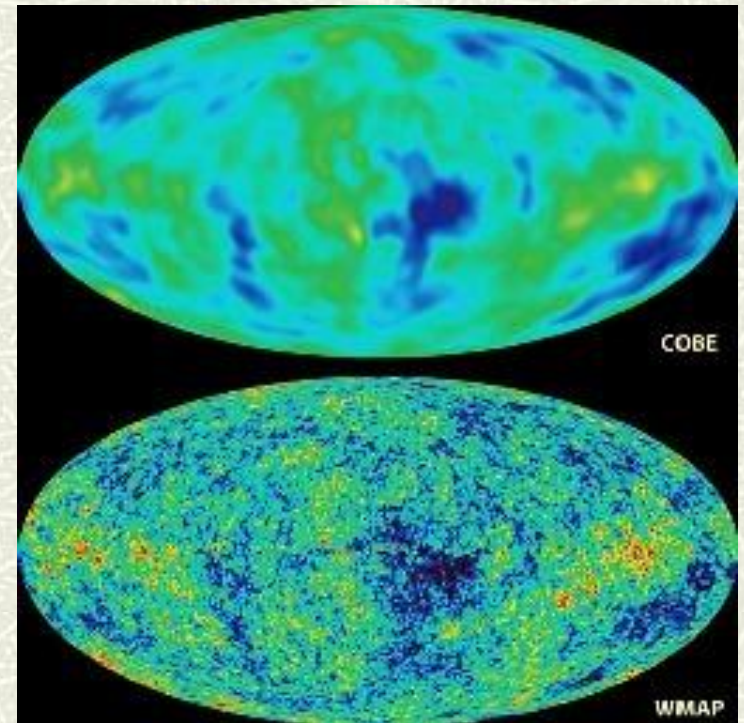
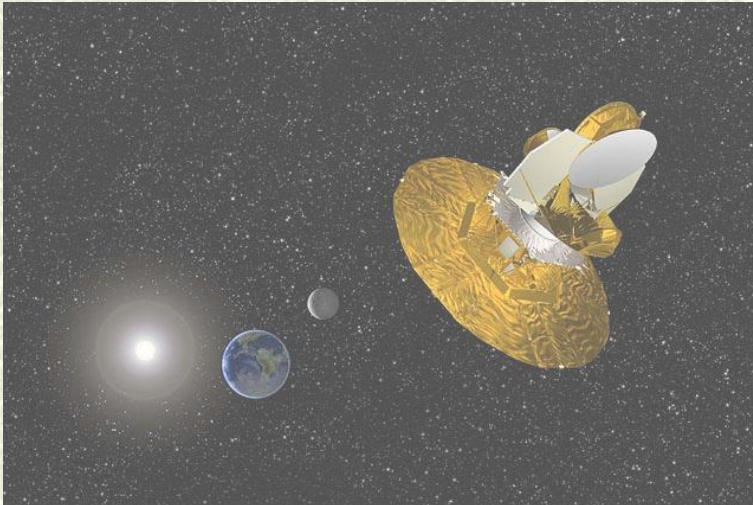
The flat universe (2000)

- Balloon measurements of CMB
- The BOOMERANG experiment
- The MAXIMA experiment
- Geometry is flat ($\Omega = 1$)
Implies dark energy component
$$\Omega_M + \Omega_\lambda = 1 \quad (\Omega_\lambda = 0.7)$$
- Support for inflation



WMAP Satellite (2002)

- Details of *CMB* spectrum
- Details of galaxy formation
- Details of flatness of U
- Details of dark energy



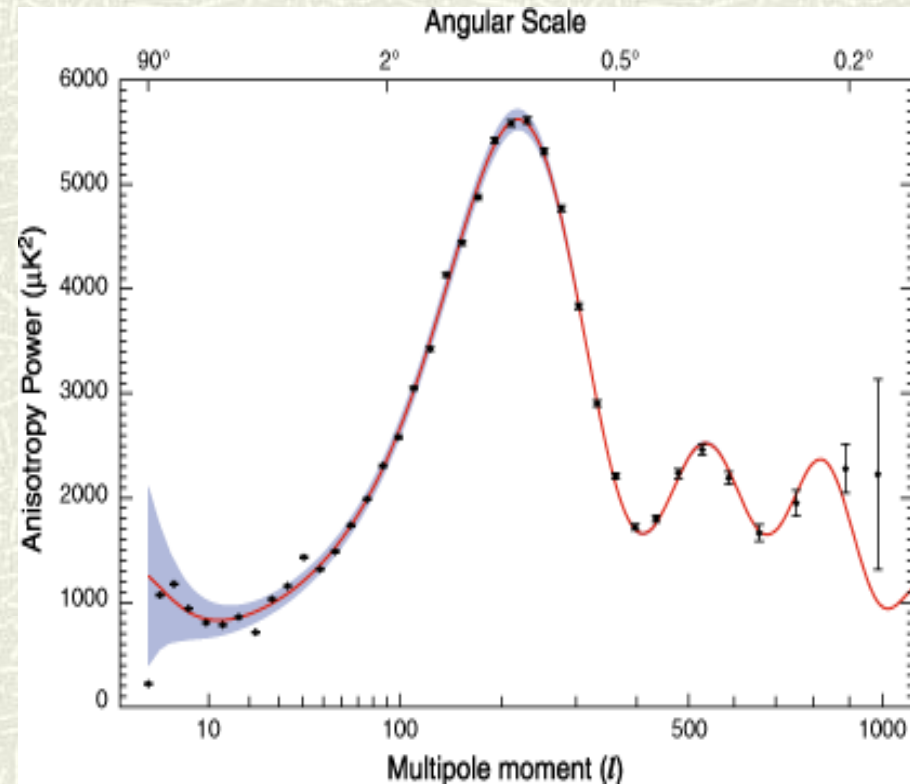
Cosmic microwave background

WMAP measurements of CMB (2005)

- Spectrum of T variations
- Geometry is flat (to 1%)
- Dark energy 74%

Strong support for dark energy

Strong support for inflation

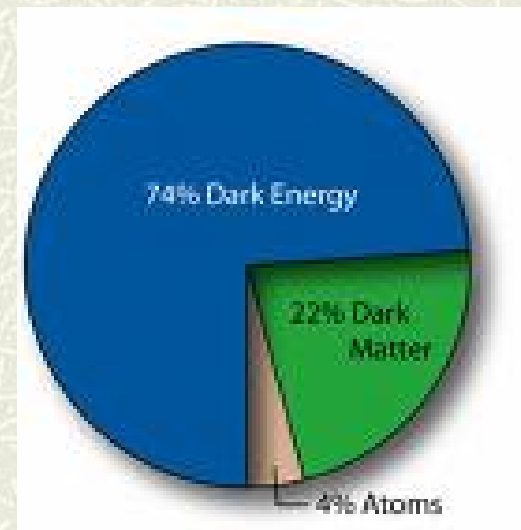


Fit to theory

Modern big bang model: Λ -CDM

A flat, accelerating universe containing matter, dark matter and dark energy

1. Ordinary matter: 4% (astrophysics)
2. Dark matter: 22% (astrophysics)
3. Dark energy : 74% (supernova, CMB)

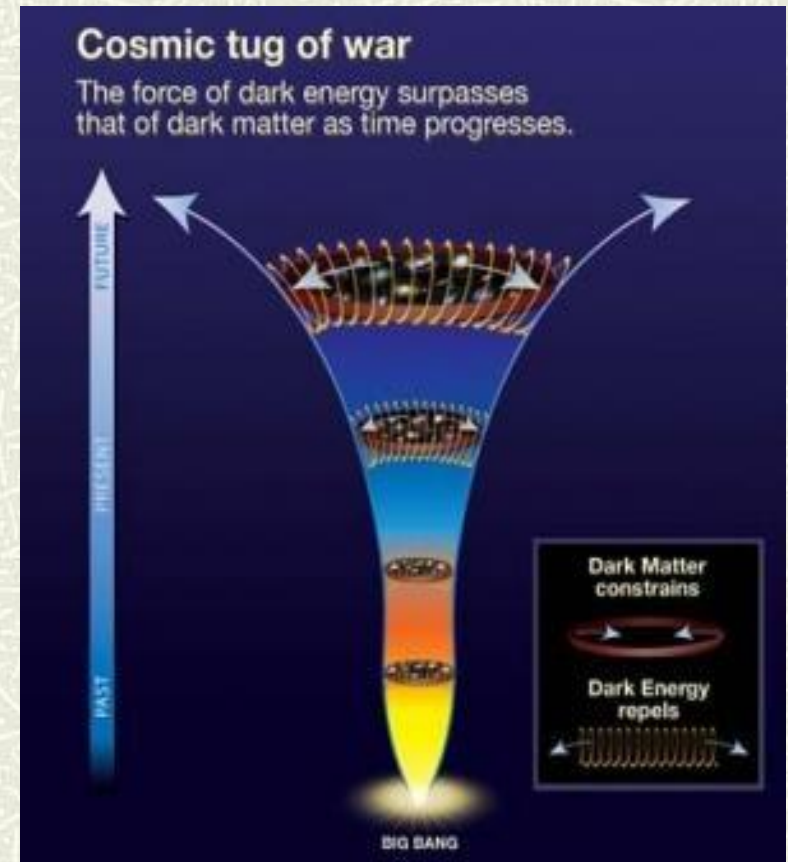


Λ CDM

$$\Omega = 1$$

Cause of acceleration: dark energy

- ⌘ Predicted by relativity
- ⌘ Cosmological constant
- ⌘ Natural tendency of space to expand
- ⌘ Energy of vacuum?
- ⌘ Why so small?
- ⌘ Why of similar density to matter?
- ⌘ Not well understood
- ⌘ Fate of universe?



New results: Planck Satellite (ESA, 2013)

1. Improved sensitivity

$$\Delta T/T \approx 1 \times 10^{-6}$$

2. Full spectrum of T anisotropy

New acoustic peaks :scale invariance?

Accurate values for Ω_{Λ} , Ω_{M}

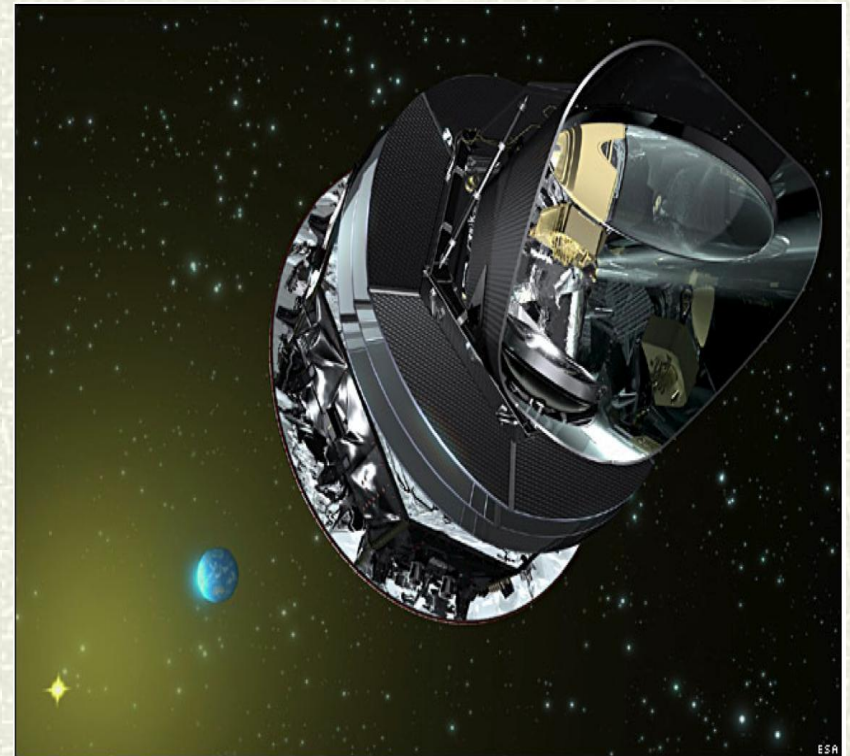
3. Gravitational lensing

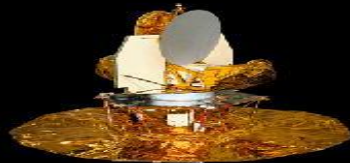
Remove degeneracies

4. Polarization measurements

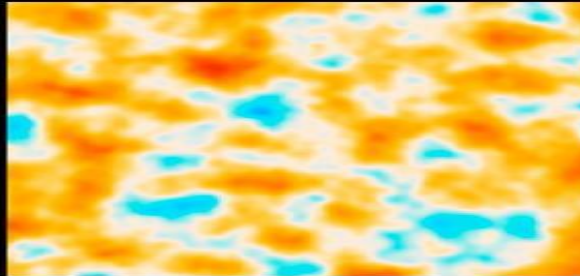
E-modes: fluctuations

B-modes: gravity waves?

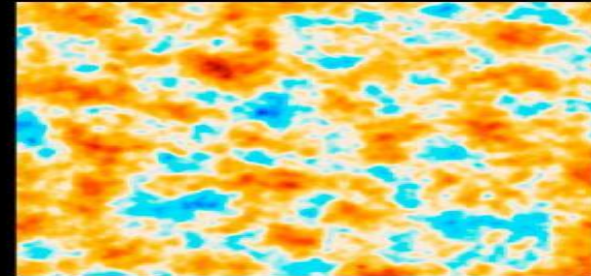




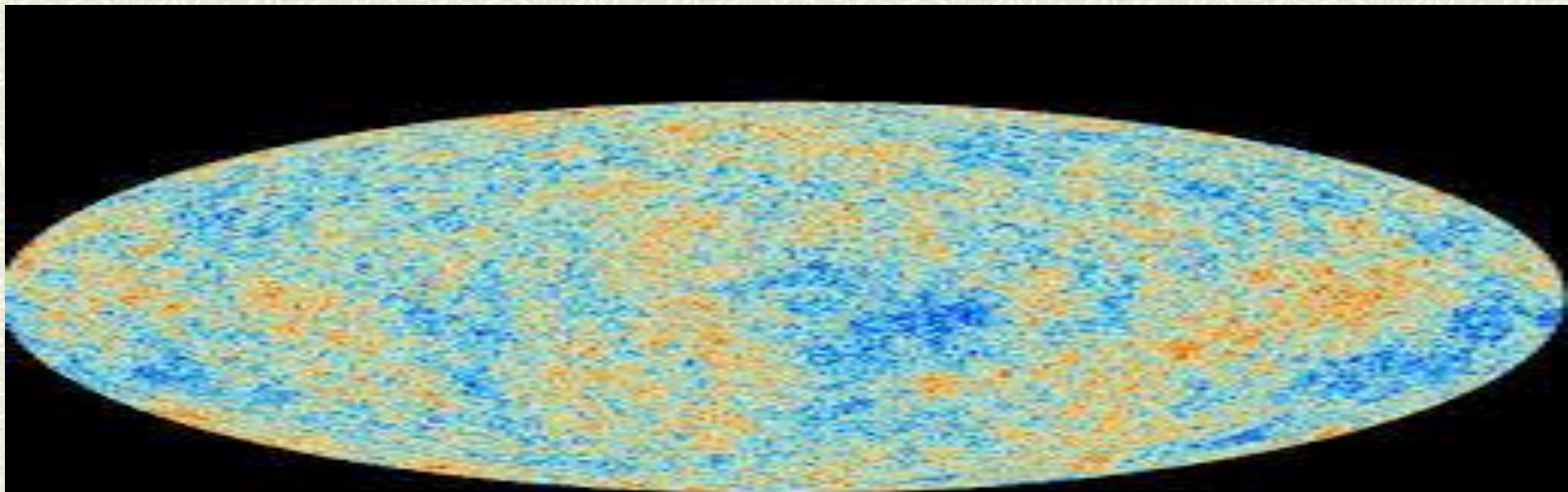
COBE



WMAP



Planck

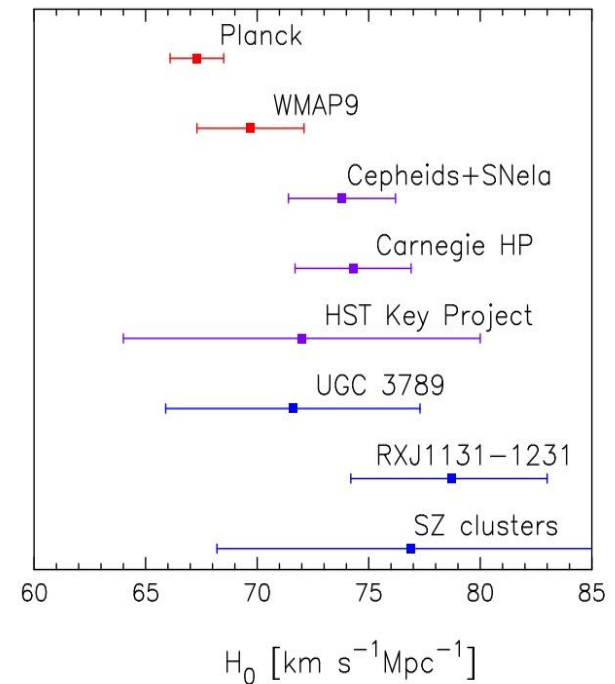


Planck results (2013)

1. New Hubble constant

$67.3 \pm 1.2 \text{ km/s/MPC}$

$\text{Age} = 13.8 \text{ billion yr}$

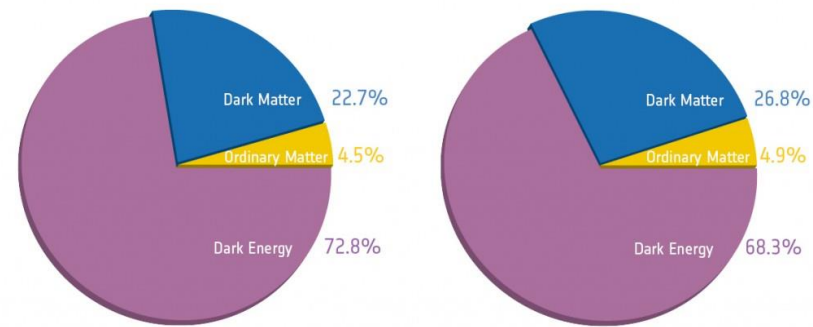


2. Curvature ; flat

$$\Omega_k = -0.0005 \pm .07$$

3. New mass/energy parameters

$$\Omega_\Lambda = 68, \Omega_{\text{DM}} = 27, \Omega_{\text{OM}} = 4.9 \%$$



Before Planck

After Planck

The big bang - problems

- ⌘ Nature of dark energy?

Role in BB?

- ⌘ Which model of inflation?

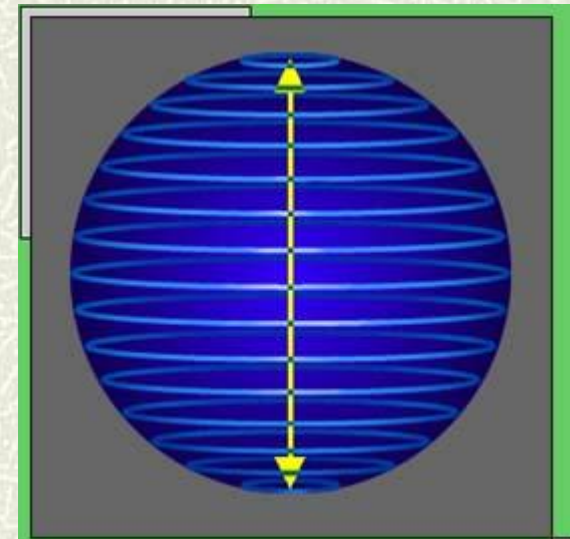
The multiverse?

- ⌘ The singularity problem

What banged?

What does time zero mean?

No-boundary universe



The no-boundary universe

- Apply quantum physics to spacetime

Quantum gravity

- Hawking/Hartle state (1983)

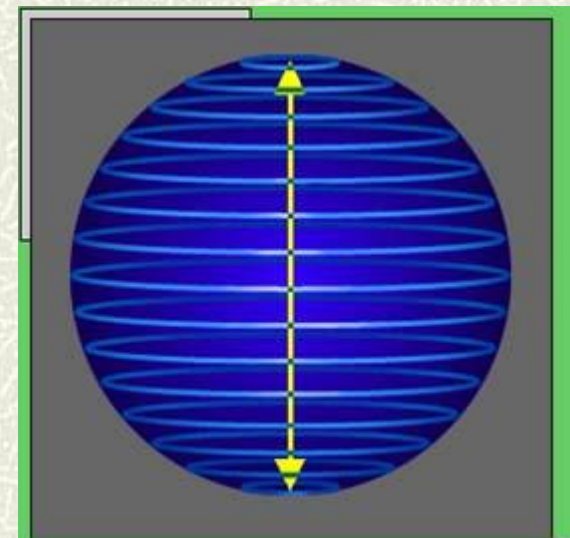
No spacetime singularity

- No boundary in time

Time does not exist before Planck era

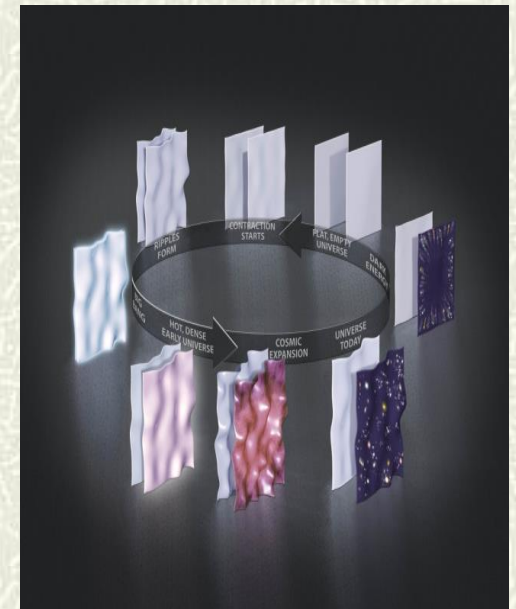
Spacetime smeared out

“What is north of the North Pole?”



The singularity: a cyclic universe?

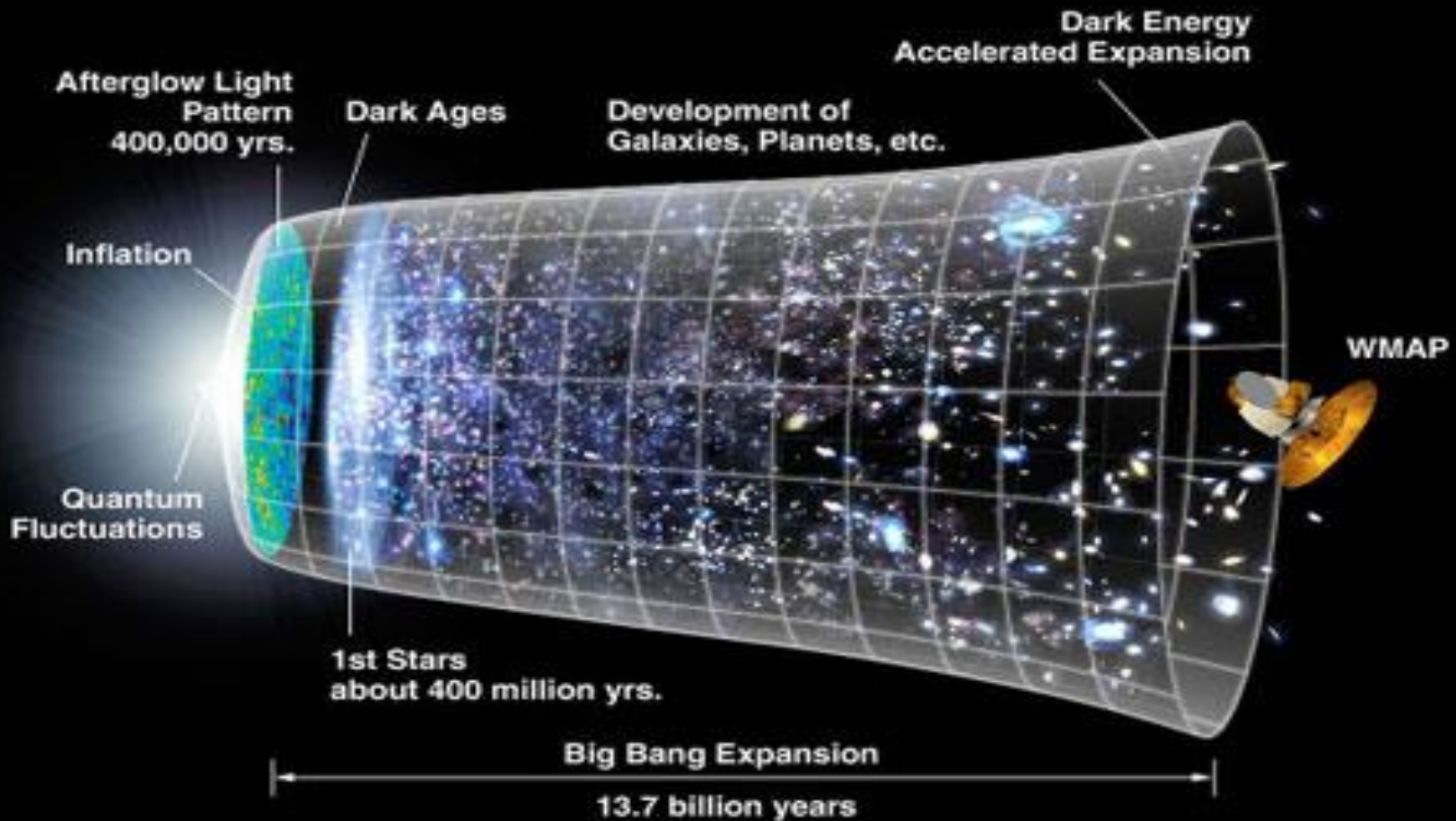
- ⌘ Breakdown at time zero
- ⌘ No model of bang itself
- ⌘ Multiple bangs?
- ⌘ Colliding branes
- ⌘ Prediction of string theory
- ⌘ Cyclic universe
- ⌘ Eternal universe



Cyclic universe

Tests? Non-Gaussianities in CMB

The big bang model



Where next for general relativity?

More general theory

Unified field theory; the forces of nature (Einstein)

Reconcile GR with quantum theory

Quantum gravity

Some progress

Black hole thermodynamics

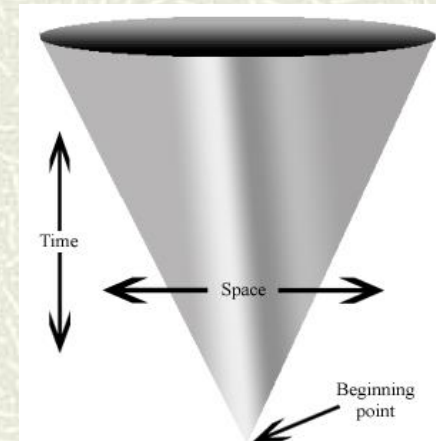
Hawking-Bekenstein radiation

Quantum cosmology

The quantum big bang

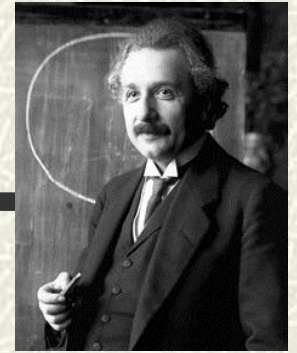


Stephen Hawking



A universe from nothing?

Einstein's cosmology: conclusions



Major test for general relativity

Conscious of assumptions of homogeneity, isotropy

Embraces dynamic cosmology

New evidence – new models (JMK)

Timespan of expanding models puzzling

Steady-state universe?

Evolving models (less contrived)

Cosmic constant not necessary

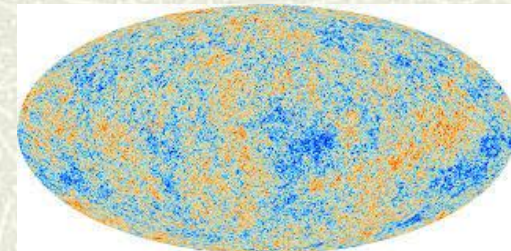
Extraction of parameters compatible with observation

Closed and open models

Timespan problem attributed to simplifying assumptions



Hubble constant revised



Cosmic microwave background
Homogeneous, flat universe

Verdict (1933, 1945): more observational data needed

No mention of origins

Einstein's lost theory uncovered

Physicist explored the idea of a steady-state Universe in 1931.

Daide Castelvechi

24 February 2014

New Discovery Reveals Einstein Tried To Devise A Steady State Model Of The Universe

2 comments, 2 called-out + Comment Now + Follow Comments

Almost 20 years before the late Fred Hoyle and his colleagues devised the [Steady State Theory](#), Albert Einstein toyed with a similar idea: that the universe was eternal, expanding outward with a consistent input of spontaneously generating matter.

An Irish physicist came across the paper last year and could hardly believe. According to this week's article in [Nature](#),

model of the universe very different to today's [Big Bang](#) Theory.

The manuscript, which hadn't been referred to by scientists for decades,



Einstein's Lost Theory Uncovered

The famous physicist explored the idea of a steady-state universe in 1931

nature

Feb 25, 2014 | By Daide Castelvechi and Nature magazine

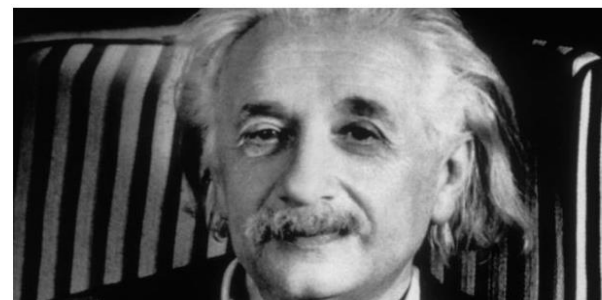
A manuscript that lay unnoticed by scientists for decades has revealed that Albert Einstein once dabbled with an



www.irishtimes.com/news/science/wit-researchers-discover-lost-einstein-model-of-universe-1.1713487

WIT researchers discover 'lost' Einstein model of universe

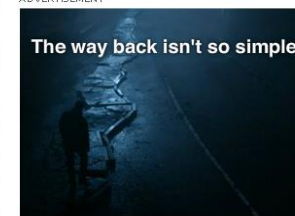
Scientists uncovered misfiled papers while searching Jerusalem university's online archive



Latest Ireland »

- 12:26 Quinn confirms Flannery approached him with Rehab concerns
- 09:07 Man in his twenties stabbed in north Dublin
- 09:05 Family hope public appeal will help daughter beat cancer
- 08:42 Gardaí investigate death of woman in Dublin
- 08:25 Flannery faces call from all parties to attend PAC

ADVERTISEMENT



III Astronomy and the Universe

The Great Debate (1900-1925)

Spiral nebulae = galaxies beyond Milky Way?

The Hooker telescope (1917)

Edwin Hubble (1921)

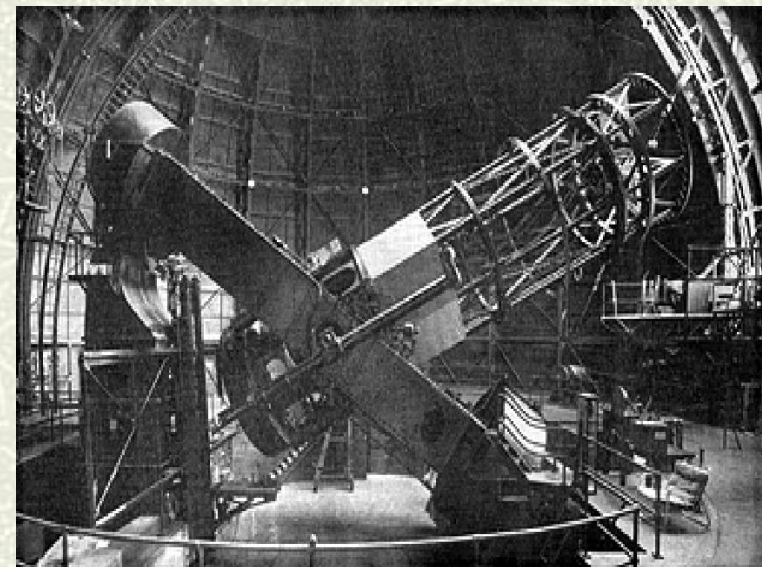
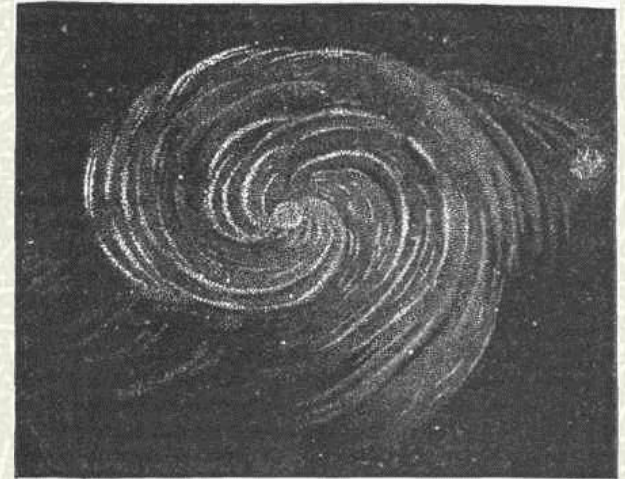
The distances of the nebulae (1925)

Cepheid variables resolved in two nebulae

Leavitt's period-luminosity relation

Spirals far beyond Milky Way

A universe of galaxies



The runaway galaxies (1929)



Edwin Hubble (1889-1953)

- **A relation between redshift and distance for the galaxies?**

- **Combine 24 distances with redshifts**

Redshifts from Slipher: not acknowledged

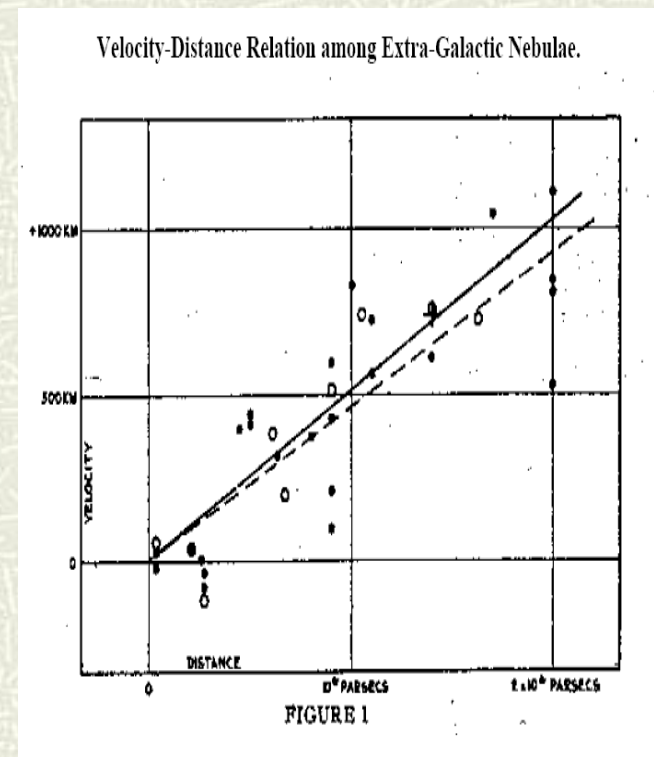
- **Linear relation: Hubble's law (1929)**

$$v = H_0 d \quad \text{with } H = 500 \text{ kms}^{-1} \text{Mpc}^{-1}$$

- **Landmark result in astronomy**

*Far-away galaxies rushing away
at a speed proportional to distance*

Why ?



Lemaître's universe (1927)



Fr Georges Lemaître

✚ Expanding model of the cosmos from GR

Similar to Friedman 1922 model

Starts from static Einstein universe

✚ Recession of nebulae = expansion of space?

Redshifts from Slipher, distances from Hubble

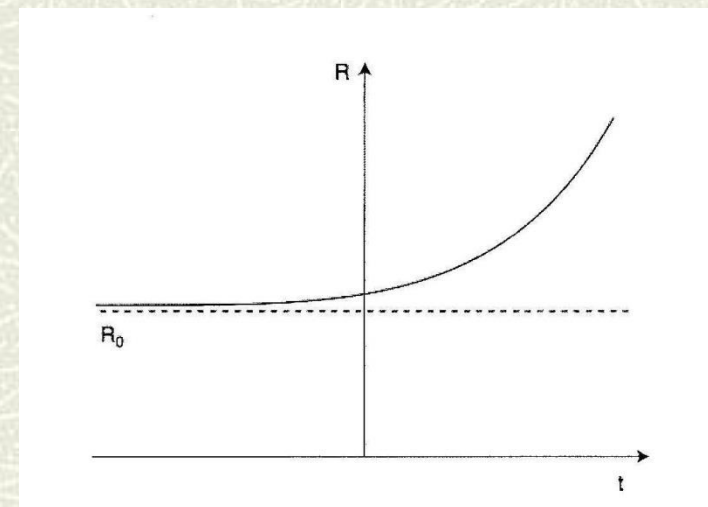
$$H = 585 \text{ kms}^{-1} \text{Mpc}^{-1}$$

✚ Ignored by community

Belgian journal (in French)

Rejected by Einstein: "Votre physique est abominable"

Einstein not up-to-date with astronomy?



The expanding universe (1930)

- **RAS meeting (1930)**

Eddington, de Sitter

If redshifts are velocities, and if effect is non-local

Static cosmic models don't match observations

- **Expanding universe?**

Hubble's law = expansion of space?

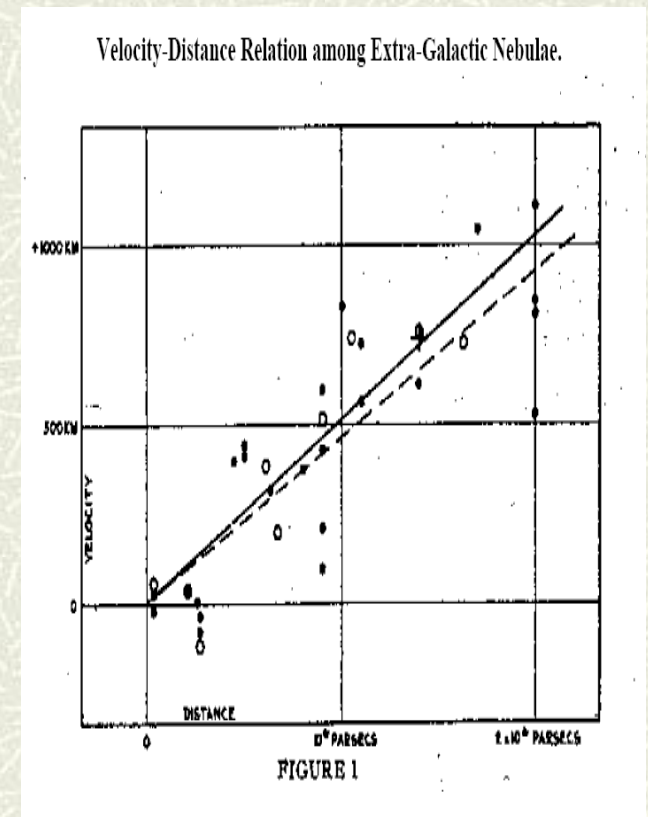
$$H = 500 \text{ kms}^{-1} \text{Mpc}^{-1}$$

- **Friedman-Lemaître model circulated**

Time-varying radius

Time-varying density of matter

Evolving universe



Models of the expanding universe (1930 -)

- **Eddington (1930, 31)**

*On the instability of the Einstein universe
Expansion caused by condensation?*

- **Tolman (1930, 31)**

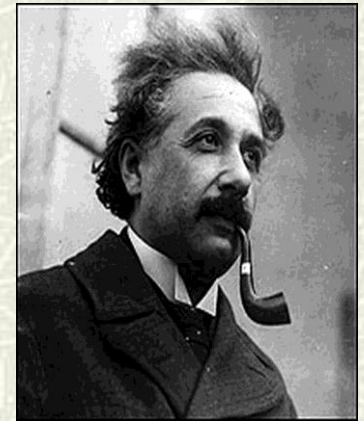
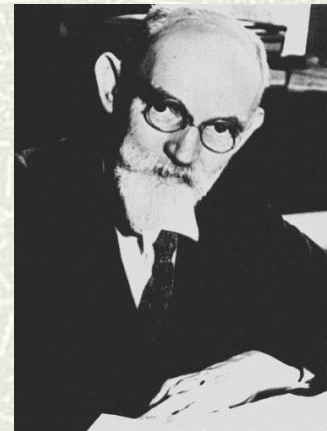
*On the behaviour of non-static models
Expansion caused by annihilation of matter ?*

- **de Sitter (1930, 31)**

*Further remarks on the expanding universe
Expanding universes of every flavour*

- **Einstein (1931, 32)**

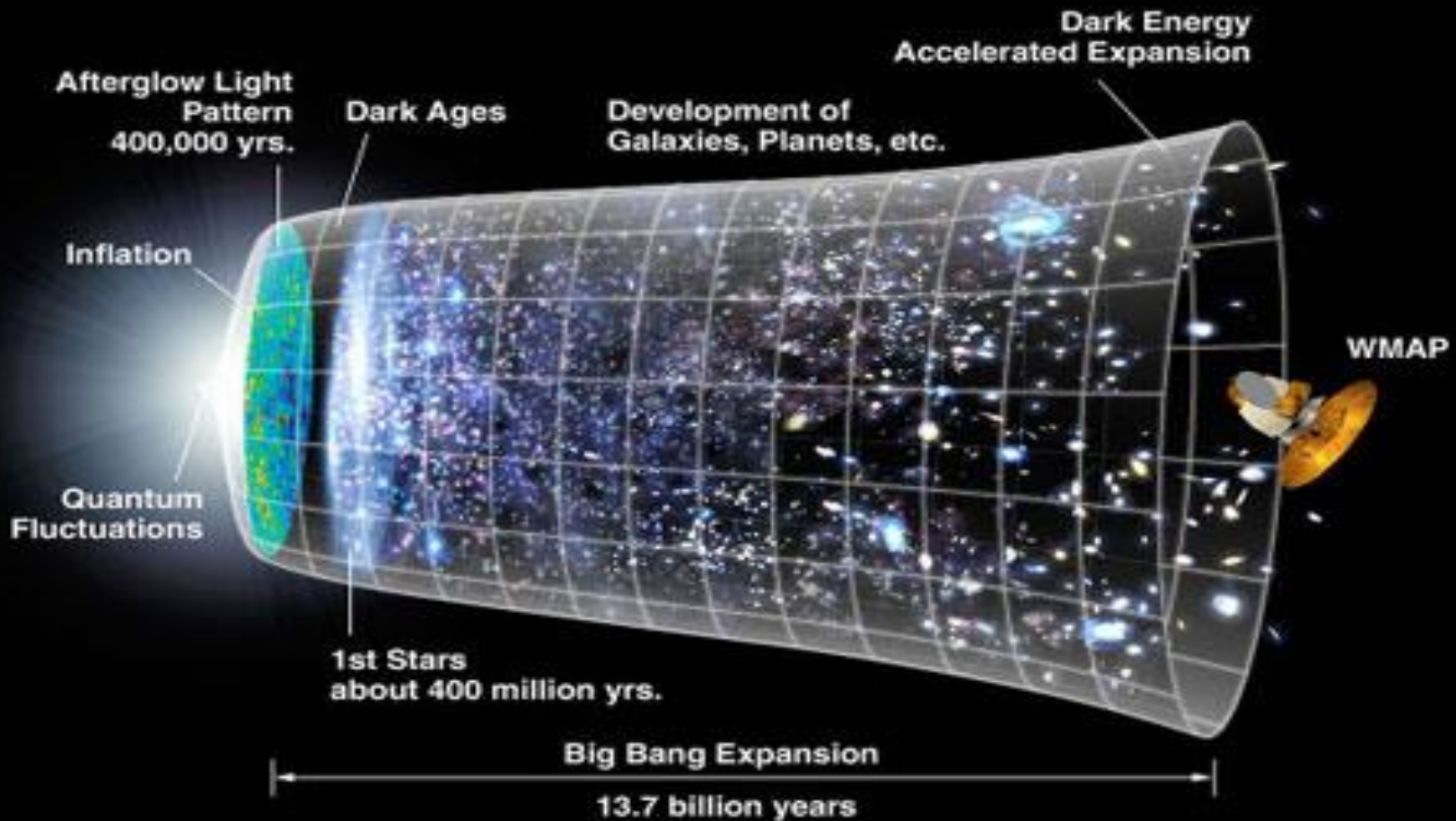
*Friedman-Einstein model $\lambda = 0, k = 1$
Einstein-de Sitter model $\lambda = 0, k = 0$*



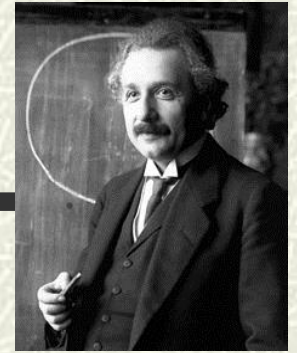
Occam's razor?

*Evolving models
No mention of origins*

The big bang model



Einstein's universe: conclusions



Cosmology = test for general relativity

Introduces λ -term to the field equations

Embraces dynamic cosmology

New evidence – new models

Steady-state vs evolving universe

Evolving models simpler: remove λ -term

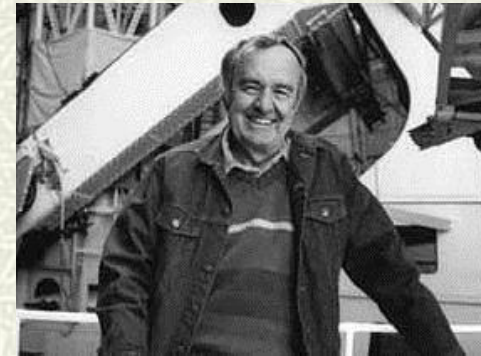
The evolving universe

Extract observational parameters

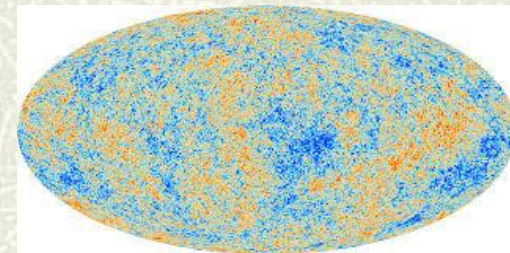
Timespan problem attributed to simplifying assumptions

No discussion of origins

Wary of extrapolations



Hubble constant revised



Cosmic microwave background
Homogeneous, flat universe

Einstein's steady-state model: key quotes

New solution

“In what follows, I wish to draw attention to a solution to equation (1) that can account for Hubbel's facts, and in which the density is constant over time”

Matter creation

“If one considers a physically bounded volume, particles of matter will be continually leaving it. For the density to remain constant, new particles of matter must be continually formed within that volume from space “

Dark energy

“The conservation law is preserved in that, by setting the λ -term, space itself is not empty of energy; its validity is well known to be guaranteed by equations (1).”

Einstein's steady-state theory: a significant find?

✦ New perspective on steady-state theory (1950s)

Logical possibility: not a crank theory

✦ Insight into scientific progress

Evolution of successful theories

No Kuhnian paradigm shift to 'big bang' model

Slow dawning

✦ Insight into Einstein's philosophy

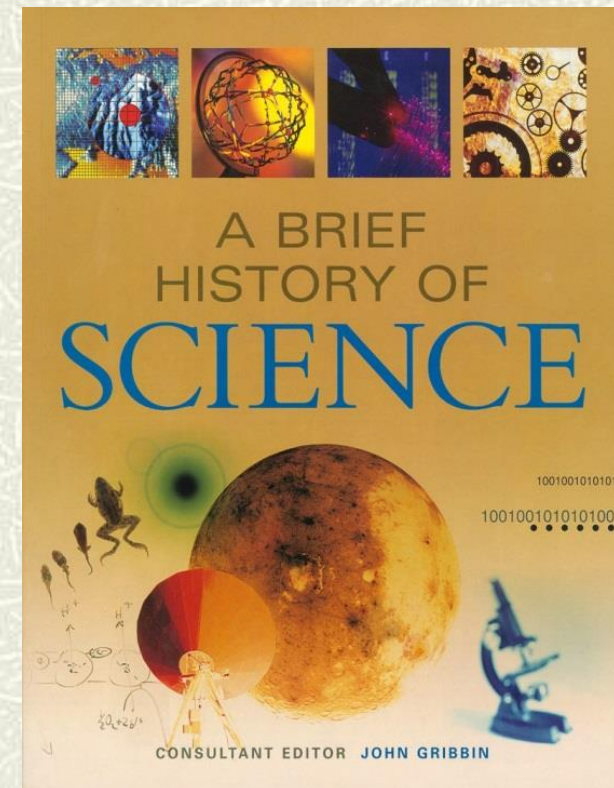
Simple solution?

Discards model rather than introduce new term to GFE

Occam's razor approach

✦ Links with modern cosmology

Dark energy, cosmic inflation



*Paradigm shift or
slow dawning ?*

Explanation for runaway galaxies?

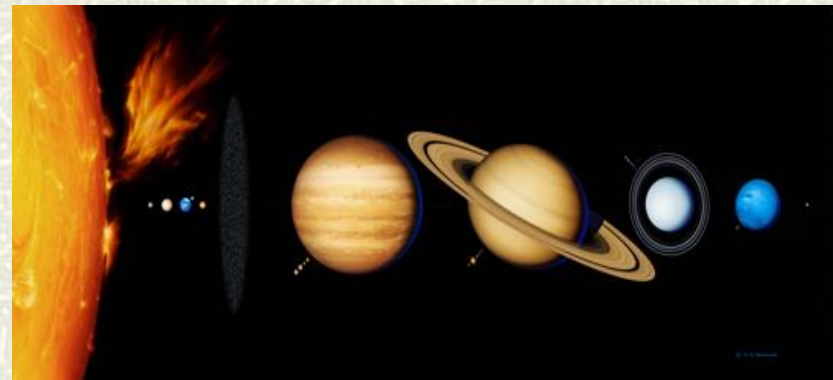
Newton

- Gravity pulls in not out
- Space is fixed
- Time has no beginning



Isaac Newton

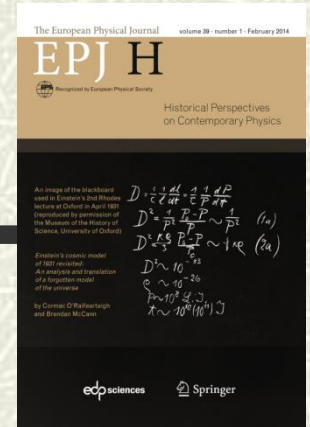
*How can galaxies be receding?
What is pushing out?*



Results: publications

■ Einstein's 1931 model

Einstein's cosmic model of 1931 revisited; an analysis and translation of a forgotten model of the universe. O'Raifeartaigh, C. and B. McCann. 2014 **Eur. Phys. J (H)** 39(1):63-85



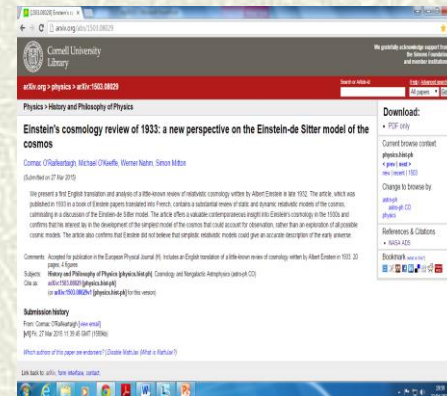
■ Einstein's steady-state manuscript

Einstein's steady-state theory: an abandoned model of the cosmos. O'Raifeartaigh, C., B. McCann, W. Nahm and S. Mitton. 2014 **Eur. Phys. J (H)** 39(3):353-367



■ Einstein-de Sitter model

Einstein's cosmology review of 1933: a new perspective on the Einstein-de Sitter model of the cosmos. O'Raifeartaigh, C., M.O'Keeffe, W. Nahm and S. Mitton. 2015. To be published in **Eur. Phys. J (H)**



■ Review paper: conclusions

ORIGINS OF THE EXPANDING UNIVERSE:
1912–1932



Edited by
Michael J. Way and Deidre Hunter

Einstein's cosmic model of 1931 revisited:
an analysis and translation of a forgotten
model of the universe

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Received 21 September 2013 / Received in final form 20 December 2013
Published online 4 February 2014
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Abstract. We present an analysis and translation of Einstein's 1931 paper "Zum kosmologischen Problem der allgemeinen Relativitätstheorie" or "On the cosmological problem of the general theory of relativity". In this little-known paper, Einstein proposes a cosmic model in which the universe undergoes an expansion followed by a contraction, quite different to the monotonically expanding Einstein-de Sitter model of 1932. The paper offers many insights into Einstein's cosmology in the light of the first evidence for an expanding universe and we consider his views of issues such as the curvature of space, the cosmological constant, the singularity and the timespan of the expansion. A number of original

An image of the blackboard
used in Einstein's 2nd Rhodes
lecture at Oxford in April 1931
(reproduced by permission of
the Museum of the History of
Science, University of Oxford)

$$D = \frac{1}{c} \frac{d\lambda}{dt} = \frac{1}{c} \frac{dP}{dP} \frac{dP}{d\tau} \\ D^2 = \frac{1}{P^2} \frac{P_0 - P}{P} \sim \frac{1}{P^2} \quad (1a) \\ D^2 = \frac{K_0}{3} \frac{P_0 - P}{P} \sim \frac{1}{P^2} \quad (2a) \\ D^2 \sim 10^{-53} \\ c \sim 10^{-26} \\ P \sim 10^8 \text{ g/cm}^3 \\ \tau \sim 10^{10} (10^{11}) \text{ s}$$

Einstein's cosmic model
of 1931 revisited:
An analysis and translation
of a forgotten model
of the universe

by Cormac O'Riartaigh
and Brendan McCann

Einstein's steady-state theory: an abandoned
model of the cosmos

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Cambridge, UK

Received 1st February 2014 / Received in final form 12 May 2014
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Abstract. We present a translation and analysis of an unpublished manuscript by Albert Einstein in which he attempted to construct a 'steady-state' model of the universe. The manuscript, which appears to have been written in early 1931, demonstrates that Einstein once considered a cosmic model in which the mean density of matter in an expanding universe is maintained constant by the continuous formation of matter from empty space. This model is very different to previously

arXiv.org > physics > arXiv:1303.08029

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arXiv:1303.08029v1 [physics.hist-ph]

Comments: Accepted for publication in the European Physical Journal (H). Includes an English translation of a little-known review of cosmology written by Albert Einstein in 1933. 20 pages, 4 figures

Subjects: History and Philosophy of Physics (physics.hist-ph); Cosmology and Nonrelativistic Astrophysics (astro-ph.CO)

Cite as: arXiv:1303.08029 [physics.hist-ph] (or arXiv:1303.08029v1 [physics.hist-ph] for this version)

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[v1] Fri, 27 Mar 2014 11:38:45 GMT (139k)

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arXiv:1304.02873v1 [physics.hist-ph]

Comments: 20 pages, 2 figures. To be published in the book 'The Philosophy of Cosmology: Foundations and Perspectives' (Cambridge University Press)

Subjects: History and Philosophy of Physics (physics.hist-ph); Cosmology and Nonrelativistic Astrophysics (astro-ph.CO)

Cite as: arXiv:1304.02873 [physics.hist-ph] (or arXiv:1304.02873v1 [physics.hist-ph] for this version)

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[v1] Sat, 11 Apr 2014 13:38:45 GMT (623k)

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Die Gleichungen (1) liefern

$$-\frac{3}{4}\alpha^2 + \lambda c^2 = 0$$

$$\frac{3}{4}\alpha^2 - \lambda c^2 = \kappa \rho c^2$$

oder

$$\alpha^2 = \frac{\kappa c^2}{3} \rho c^2 \dots (4)$$

Die Dichte ist also konstant und bestimmt die Expansion bis auf das Vorzeichen.

Taking $T_{44} = \rho c^2$ (all other components zero) in the *time* component of equation (1) we obtain $\left(R_{44} - \frac{1}{2}g_{44}R\right) - \lambda g_{44} = \kappa \rho c^2$.

This gives on analysis $-3\alpha^2/4 + 3\alpha^2/2 - \lambda c^2 = \kappa \rho c^2$ the second of Einstein's simultaneous equations.

From the *spatial* component of equation (1), we obtain $\left(R_{ii} - \frac{1}{2}g_{ii}R\right) - \lambda g_{ii} = 0$.

This gives on analysis $3\alpha^2/4 - 3\alpha^2/2 + \lambda c^2 = 0$ for the first of the simultaneous equations.

It is plausible that Einstein made a sign error here, initially getting $3\alpha^2/4 + 3\alpha^2/2 + \lambda c^2 = 0$ for this equation. (W. Nahm)

Einstein's steady-state model and cosmology today

■ Accelerated expansion (1998)

Supernova measurements

Dark energy – positive cosmological constant



■ Einstein's dark energy

“The conservation law is preserved in that, by setting the λ -term, space itself is not empty of energy; its validity is well known to be guaranteed by equations (1).”

Anticipates positive cosmological constant

■ De Sitter line element

$$ds^2 = -e^{\alpha t} (dx_1^2 + dx_2^2 + dx_3^2) + c^2 dt^2 \dots$$

Necessary for all steady-state models

Identical to inflationary models (different time-frame)

Some key quotes (Einstein 1917)

“In a consistent theory of relativity, there can be no inertia relative to “space”, but only an inertia of masses relative to one another”

“I have not succeeding in formulating boundary conditions for spatial infinity. Nevertheless, there is still a way out...for if it were possible to regard the universe as a continuum which is finite (closed) with respect to its spatial dimensions, we should have no need at all of any such boundary conditions”

“The most important fact that we draw from experience as to the distribution of matter is that the relative velocities of the stars are very small compared with the velocity of light..... There is a system of reference relative to which matter may be looked upon as being permanently at rest ”

“However, the system of equations ..allows a readily suggested extension which is compatible with the relativity postulate... For on the left hand side of the field equation...we may add the fundamental tensor $g_{\mu\nu}$, multiplied by a universal constant , $-\lambda$, at present unknown, without destroying the general covariance ”

Schroedinger's comment (1918): Einstein's response (1918)

An abandoned model

■ Correct geometry

de Sitter metric

■ Simultaneous equations

Eliminate λ

Relation between α^2 and ρ

■ Einstein's crossroads

Null solution on revision

Tolman? (Nussbaumer 2014)

Declined to amend GFE

■ Evolving models

Less contrived: set $\lambda = 0$

Im Nachfolgenden will ich auf eine Lösung der Gleichung (1) aufmerktsam machen, welche Hubble's Thatsachen gerecht wird, und in welcher die Dichte zeitlich konstant ist. Diese Lösung ist zwar in dem allgemeinen Schema Tolman's mitthalten, scheint aber bisher nicht in Betracht gezogen worden zu sein.

1. Ich setze an

$$ds^2 = -e^{\alpha t} (dx_1^2 + dx_2^2 + dx_3^2) + c^2 dt^2 \dots (3)$$

Die Gleichungen (1) liefern

$$-\frac{3}{4} \alpha^2 + \lambda c^2 = 0 \qquad 9\alpha^2 / 4 + \lambda c^2 = 0$$

$$\frac{3}{4} \alpha^2 - \lambda c^2 = \kappa \rho c^2 \qquad 3\alpha^2 / 4 - \lambda c^2 = \kappa \rho c^2$$

oder

$$\alpha^2 = \frac{\kappa c^2}{3} \rho \dots (4) \qquad \alpha^2 = \frac{\kappa c^2}{3} \rho$$

Die Dichte ist also konstant und bestimmt die Expansion bis auf das Vorzeichen.

Der Erhaltungssatz bleibt dadurch unvabrt, dass bei Setzung des λ -Gleides der Raum selbst nicht energetisch leer ist; seine Uftaltung wird bekanntlich durch die Gleichungen (1) gewahrleistet.

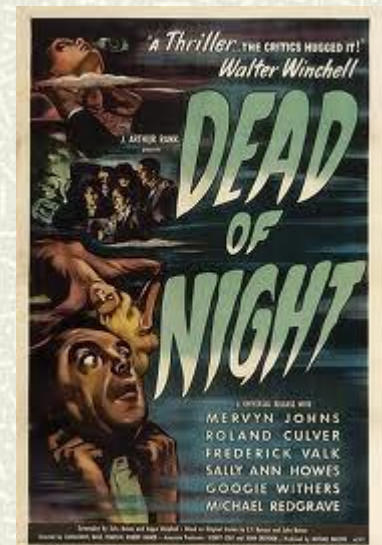
Steady-state universe (1948)

- ⌘ Alternative to big bang (*Fred Hoyle*)
- ⌘ Expanding universe

BUT

- ⌘ Continuous creation of matter?
- ⌘ Unchanging universe
- ⌘ No beginning, no age problem
- ⌘ No assumptions about early epochs

Very little matter needed



3. Einstein's steady-state model

Unpublished manuscript

Archived as draft of F-E model (1931)

Similar title, opening to F-E model

Something different

Cosmological constant

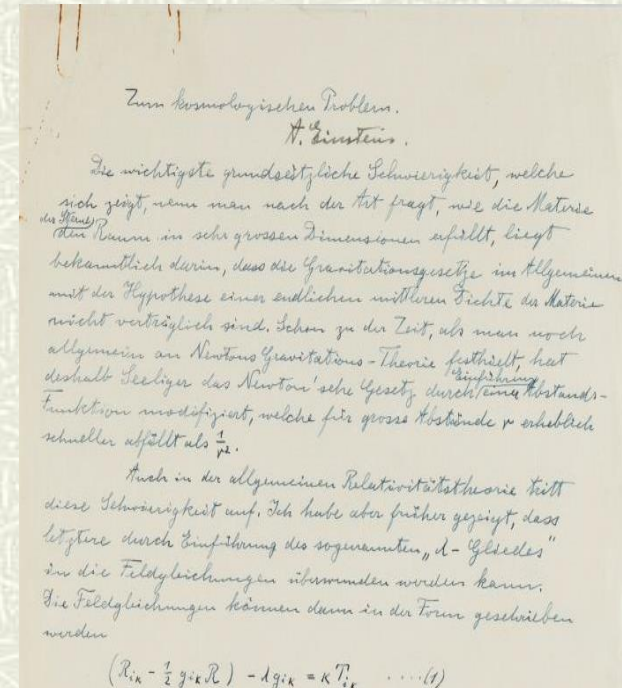
"The density is thus constant and determines the expansion"

Steady-state model of the Expanding Universe

Anticipates Hoyle solution

Written in early 1931

Fatal flaw: abandoned



Die Gleichungen (1) liefern

$$-\frac{3}{4} \alpha^2 + \Lambda c^2 = 0$$

$$\frac{3}{4} \alpha^2 - \Lambda c^2 = \kappa \rho c^2$$

$$\alpha^2 = \frac{\kappa c^2}{3} \rho \dots (4)$$

oder

$$9\alpha^2 / 4 + \Lambda c^2 = 0$$

$$3\alpha^2 / 4 - \Lambda c^2 = \kappa \rho c^2$$

$$\alpha^2 = \frac{\kappa c^2}{3} \rho$$

Die Dichte ist also konstant und bestimmt die Expansion bis auf das Vorzeichen.

Einstein's lost theory uncovered

Physicist explored the idea of a steady-state Universe in 1931.

Daide Castelvechi

24 February 2014

New Discovery Reveals Einstein Tried To Devise A Steady State Model Of The Universe

2 comments, 2 called-out + Comment Now + Follow Comments

Almost 20 years before the late Fred Hoyle and his colleagues devised the [Steady State Theory](#), Albert Einstein toyed with a similar idea: that the universe was eternal, expanding outward with a consistent input of spontaneously generating matter.

An Irish physicist came across the paper last year and could hardly believe. According to this week's article in [Nature](#),

model of the universe very different to today's [Big Bang](#) Theory.

The manuscript, which hadn't been referred to by scientists for decades,



Einstein's Lost Theory Uncovered

The famous physicist explored the idea of a steady-state universe in 1931

nature

Feb 25, 2014 | By Daide Castelvechi and Nature magazine

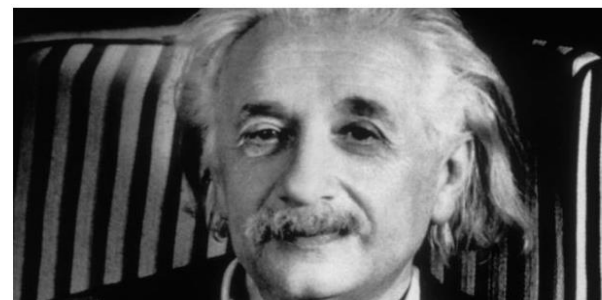
A manuscript that lay unnoticed by scientists for decades has revealed that Albert Einstein once dabbled with an



www.irishtimes.com/news/science/wit-researchers-discover-lost-einstein-model-of-universe-1.1713487

WIT researchers discover 'lost' Einstein model of universe

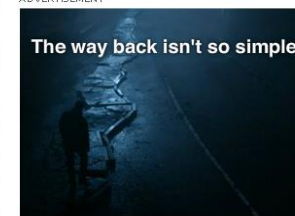
Scientists uncovered misfiled papers while searching Jerusalem university's online archive



Latest Ireland »

- 12:26 Quinn confirms Flannery approached him with Rehab concerns
- 09:07 Man in his twenties stabbed in north Dublin
- 09:05 Family hope public appeal will help daughter beat cancer
- 08:42 Gardaí investigate death of woman in Dublin
- 08:25 Flannery faces call from all parties to attend PAC

ADVERTISEMENT



2. Einstein-de Sitter model (1932)

Remove spatial curvature

Curvature not a given in dynamic models (Heckmann)

Not observed empirically (Occam's razor)

$$ds^2 = -R^2(dx^2 + dy^2 + dz^2) + c^2dt^2$$

Simplest Friedman model

Time-varying universe with $\lambda = 0$, $k = 0$, $p = 0$

Estimate of density : $\rho = 10^{-28} \text{ g/cm}^3$

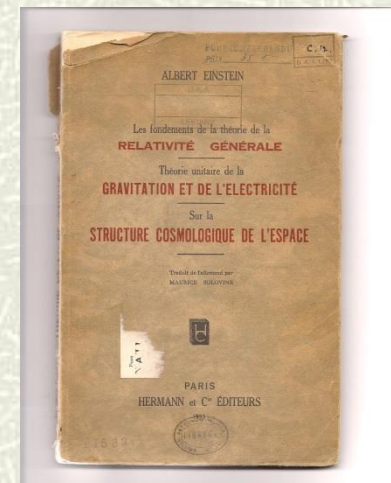
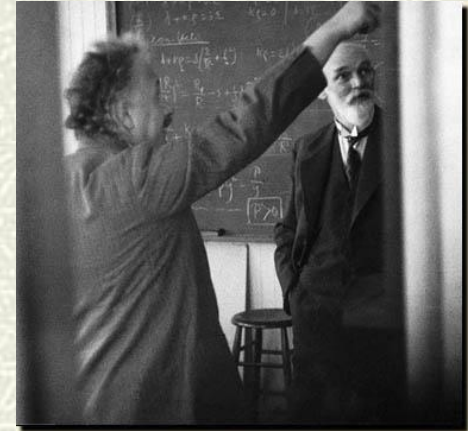
$$\frac{1}{R^2} \left(\frac{dR}{cdt} \right)^2 = \frac{1}{3} \kappa \rho.$$

Becomes standard model

Despite high density of matter, age problem

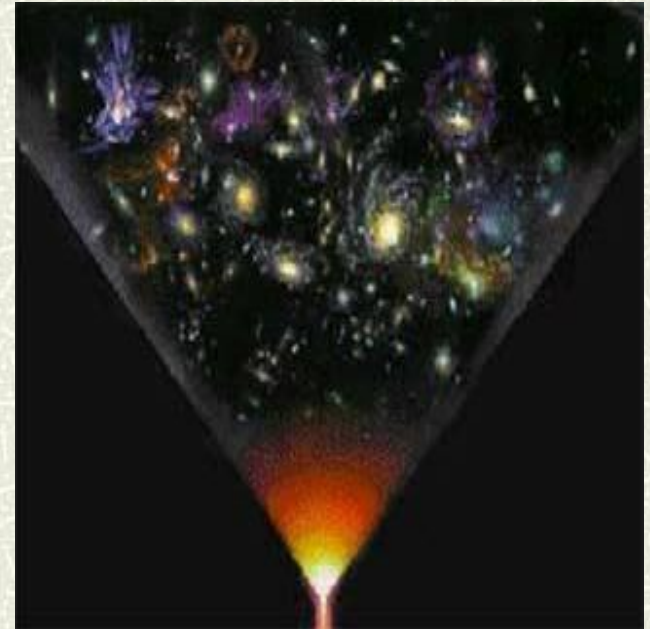
Time evolution not considered

Longer version with time evolution (Einstein 1933)



IV The 'big bang' model (1931)

- ✚ Infant U concentrated in tiny volume
- ✚ Extremely dense, hot
- ✚ Expanding and cooling ever since



Where do the laws of physics come from?

Wrong age (Hubble constant)

Singularity problem
 ∞ density, ∞ temp at $t = 0$?

Cosmic prediction I: Black Holes

Schwarzschild (1916)

Exact solution for the field equations

Body of spherical symmetry

Enigma

Solution becomes singular at $r = 2GM/c^2$

Space closed up around mass?

Rejected

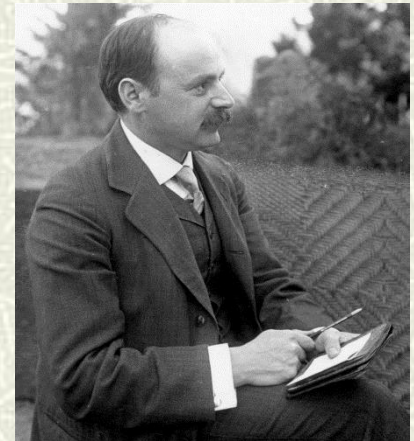
Co-ordinate problem (Eddington)

Prevented by internal pressure (Einstein 1922)

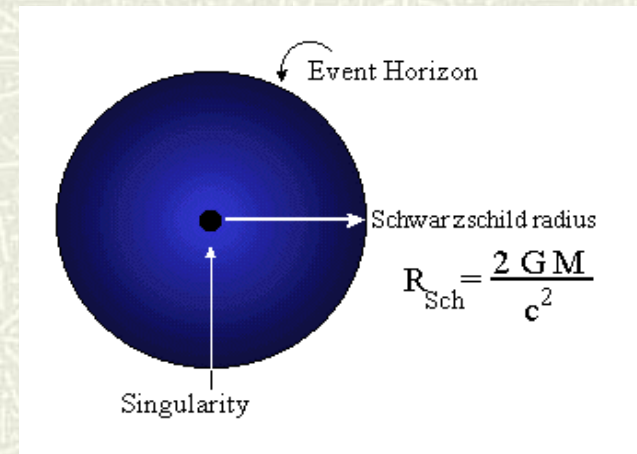
Physical reality?

Collapse of sun? Anderson (UCG)

Collapse of large stellar ensemble : Lodge (Oxford)



Karl Schwarzschild (1873–1916)



The physics of black holes

Chandrasekhar (1931)

The physics of white dwarf stars (quantum degeneracy)

SR: collapse to infinite density for $M > 1.4 M_{\odot}$

Rejected by Eddington, community



Oppenheimer (1939,40)

GR: Continued stellar collapse for $M > 3 M_{\odot}$

Rejected by Einstein (1939)

Wheeler, Thorne, Zeldovitch (1960s)

Numerical solutions of the field equations

Simulation of stellar collapse



Penrose (1965)

No avoiding BH singularity

Black Holes: Observation

Compact astronomical objects (1960s)

Quasars: small, distant sources of incredible energy (1963)

Pulsars: rapidly rotating neutron stars (1967)

X-ray binaries

Cygnus X-1 (1964)

Matter pulled from star into massive companion emits X-rays

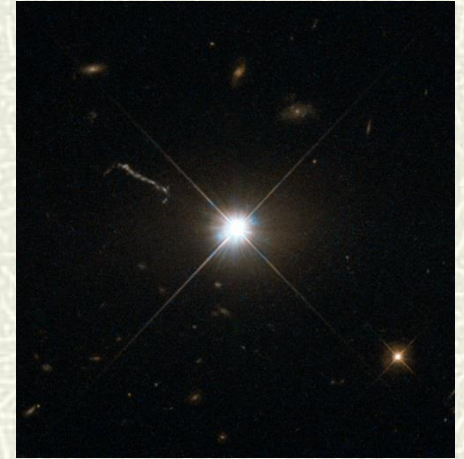
Orbit studies

Supermassive BH at centre of MW? (1990s)

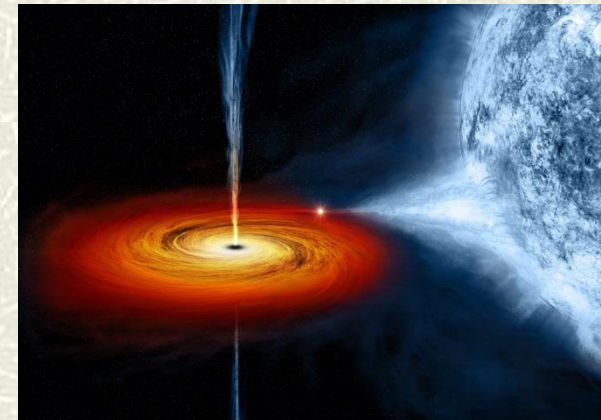
Supermassive BH at centre of many galaxies (2000-)

2015-16

Gravitational waves from binary BH system!



Quasar 3C273



Cygnus X-1 (1964)

Relativity and the universe

⌘ The field equations of general relativity (1916)

$$G_{\mu\nu} = -\kappa T_{\mu\nu}$$

⌘ Solution for the case of the universe?

Ultimate test for new theory of gravitation

⌘ Assumptions

Uniform, static distribution of matter

Closed spatial curvature

Introduce the cosmic constant λ

⌘ The Einstein World (1917)

Static universe of spherical geometry

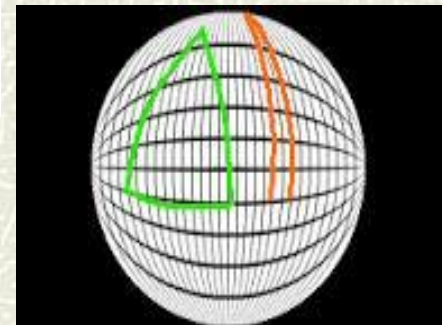
Cosmic radius and matter density defined by λ

$$G_{\mu\nu} + \lambda g_{\mu\nu} = -\kappa T_{\mu\nu}$$

$$\lambda = \frac{\kappa\rho}{2} = \frac{1}{R^2}$$



The Einstein World



Big bang puzzles

⌘ Characteristics of background radiation

Homogeneity, flatness, galaxy formation?(1970-80)

⌘ The theory of inflation (1981)

Exponential expansion within first second?

Initial conditions?

Which model of inflation?

⌘ Dark energy (1998)

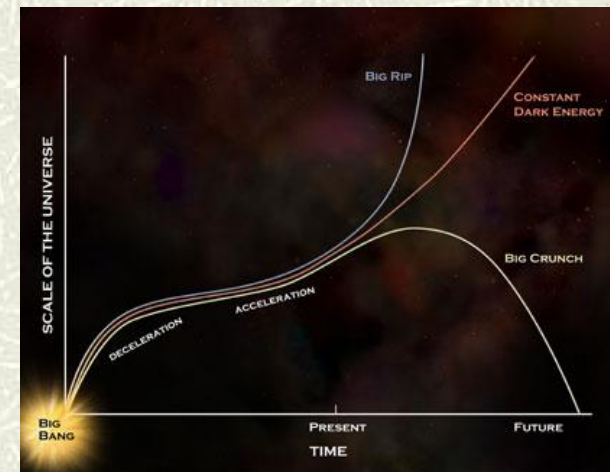
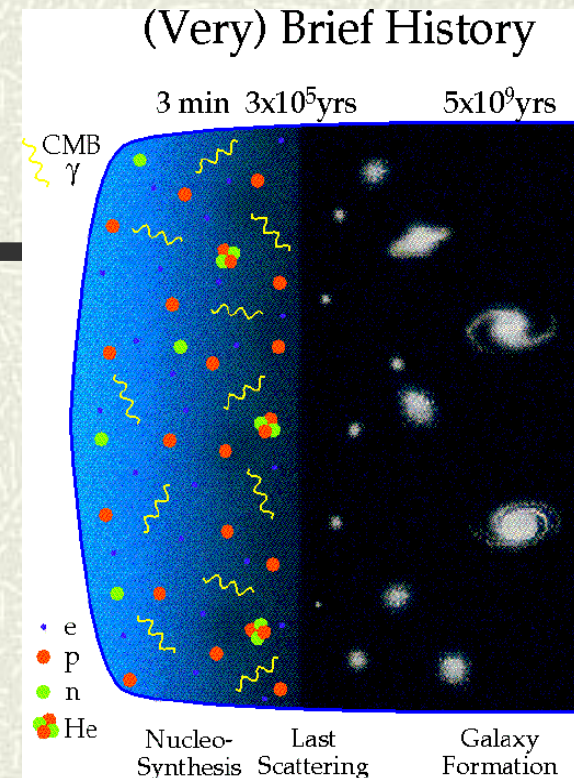
Observation of accelerated expansion

The return of the cosmological constant

Problems of interpretation

$$G_{\mu\nu} + \lambda g_{\mu\nu} = -\kappa T_{\mu\nu}$$

Nature of DE unknown



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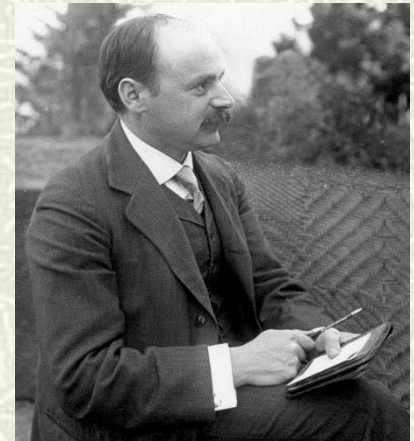
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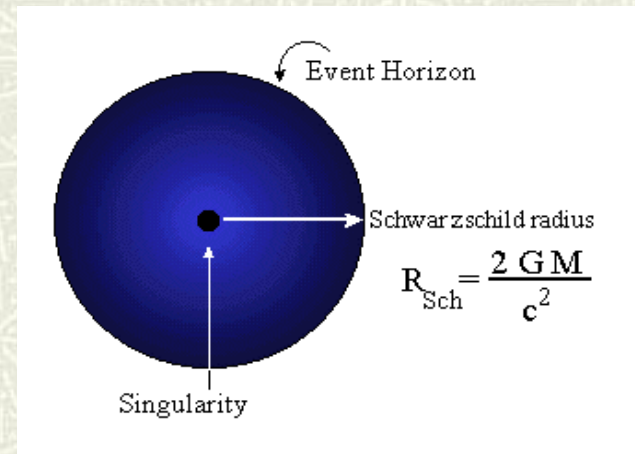
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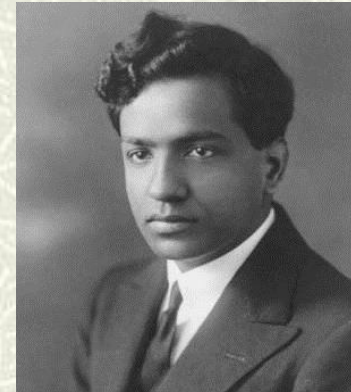
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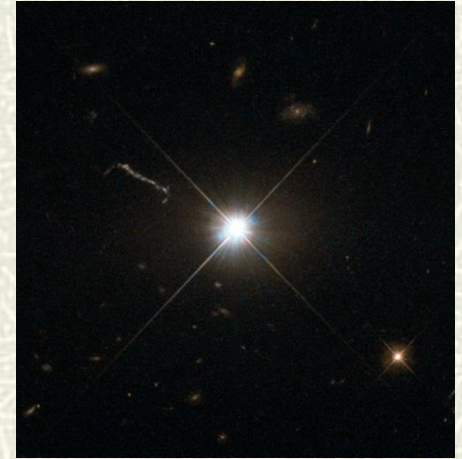
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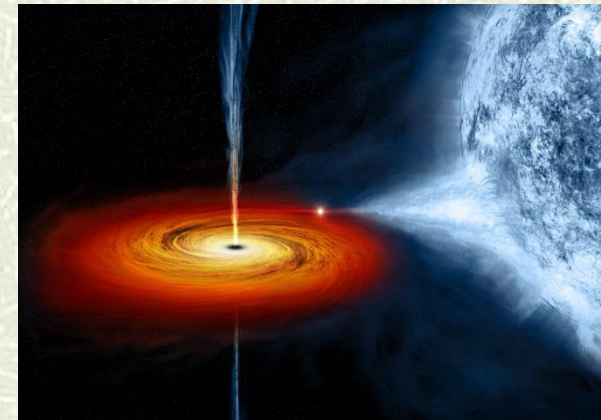
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■ **2015-16**

Gravitational waves from BH merger!



Quasar 3C273



Cygnus X-1 (1964)

Three astronomical tests (Einstein, 1916)

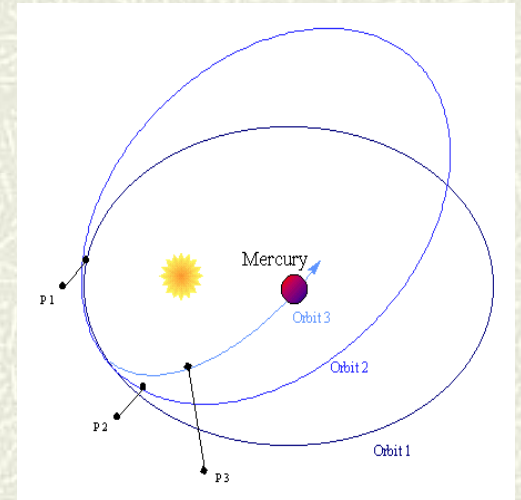
⌘ Different in principle from Newton's gravity

Small deviations in practice (weak scale)

⌘ The perihelion of Mercury

Well-known anomaly in Mercury's orbit (43" per century)

Postdicted by GR (1916)



⌘ The bending of starlight by the sun (1.7")

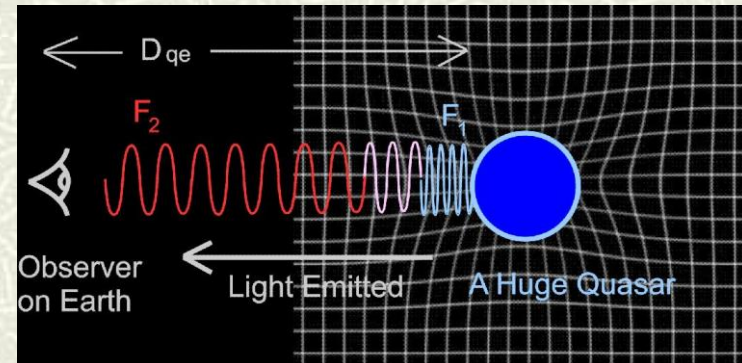
Eclipse expeditions of Eddington and Dyson (1919)

Successful measurement (large error margin)

⌘ Gravitational redshift

Time dilation in strong gravitational field

Light from a star redshifted by stellar mass?



Problems with standard model (1980-1998)

✦ Einstein-de Sitter: $\lambda = 0, k = 0$

✦ Flatness prediction (Dicke, inflation)

$$k = 0$$

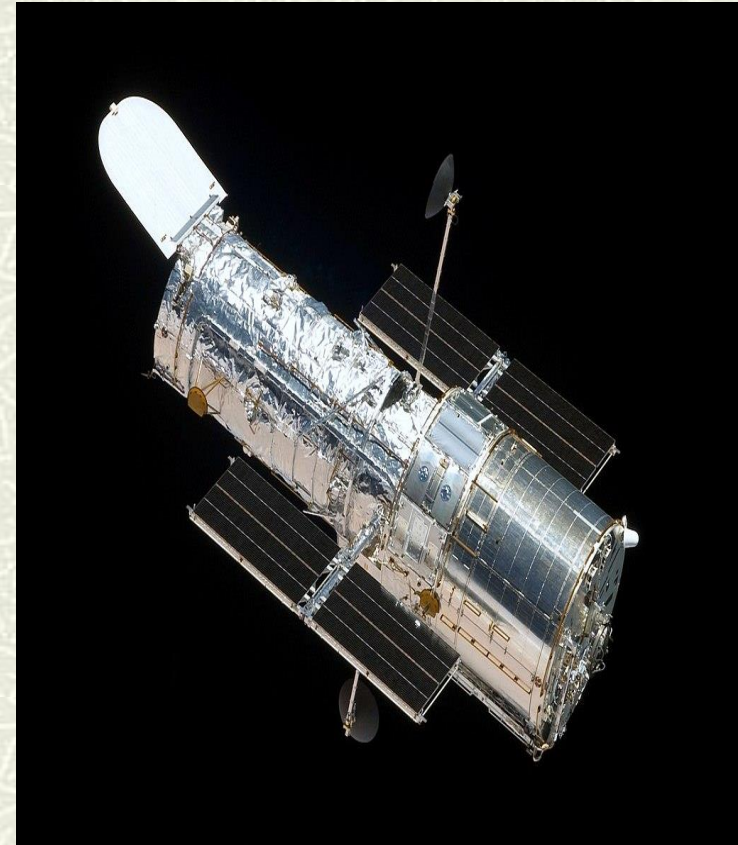
✦ But: $\Omega_M = 0.3$

✦ But: new timescale problem from HST

$$H = 87 \text{ kms}^{-1} \text{ Mpc}^{-1} : t = 11.2 \times 10^9 \text{ yr}$$

too young

Is model wrong? Is $\lambda \neq 0$?



*Hubble Space Telescope
1990*