

Einstein's Universe

General relativity and the big bang

Cormac O'Raifeartaigh FRAS

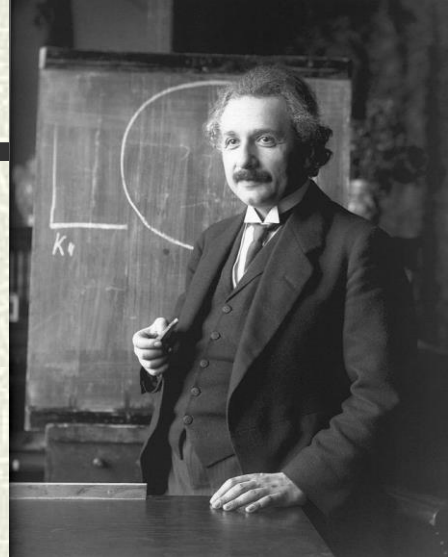
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Overview

▣ 100 years of general relativity

The special theory of relativity

The general theory of relativity



▣ General relativity and the universe

The expanding universe

The big bang model

Einstein in California (1931)

▣ Einstein's universe

Some new findings



100 years of general relativity



First formulation of the equations of GR (1915)

First full formulation of the theory of GR (1916)

844 Sitzung der physikalisch-mathematischen Klasse vom 25. November 1915

Die Feldgleichungen der Gravitation.

VON A. EINSTEIN.

In zwei vor kurzem erschienenen Mitteilungen^[1] habe ich gezeigt, wie man zu Feldgleichungen der Gravitation gelangen kann, die dem Postulat allgemeiner Relativität entsprechen, d. h. die in ihrer allgemeinen Fassung beliebigen Substitutionen der Raumzeitvariablen gegenüber kovariant sind.

Der Entwicklungsgang war dabei folgender. Zunächst fand ich Gleichungen, welche die NEWTONSCHE Theorie als Näherung enthalten und beliebigen Substitutionen von der Determinante ϵ gegenüber kovariant waren. Hierauf fand ich, daß diesen Gleichungen allgemein kovariante entsprechen, falls der Skalar des Energietensors der „Materie“ verschwindet. Das Koordinatensystem war dann nach der einfachen Regel zu spezialisieren, daß $\sqrt{-g}$ zu 1 gemacht wird, wodurch die Gleichungen der Theorie eine einuente Vereinfachung erfahren. Dabei mußte aber, wie erwähnt, die Hypothese eingeführt werden,

1916.

M. 7.

ANNALEN DER PHYSIK

VIERTE FOLGE. BAND 49.

1. Die Grundlage der allgemeinen Relativitätstheorie; von A. Einstein.

Die im nachfolgenden dargelegte Theorie bildet die denkbar weitgehendste Verallgemeinerung der heute allgemein als

[1] „Relativitätstheorie“ bezeichneten Theorie; die letztere nenne ich im folgenden zur Unterscheidung von der ersteren „spezielle

[2] Relativitätstheorie“ und setze sie als bekannt voraus. Die Verallgemeinerung der Relativitätstheorie wurde sehr erleichtert durch die Gestalt, welche der speziellen Relativitätstheorie durch Minkowski gegeben wurde, welcher Mathematiker zuerst die formale Gleichwertigkeit der räumlichen Koordinaten und der Zeitkoordinate klar erkannte und für

The special theory of relativity

■ Two new principles (1905)

Laws of physics identical for observers in uniform motion

Speed of light identical for observers in uniform motion



■ Implications

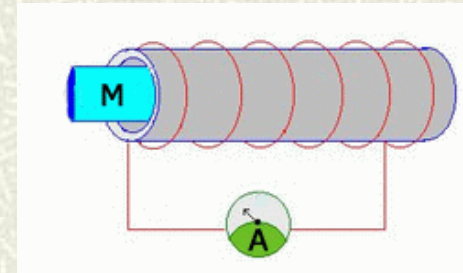
Distance and time not absolute

Distance and time not identical for bodies in uniform motion

■ Predictions for high-speed bodies

Length contraction; time dilation

Mass increase; mass-energy equivalence $E = mc^2$



■ Space + time = spacetime

$$ds^2 = dx^2 + dy^2 + dz^2 - c^2 dt^2$$

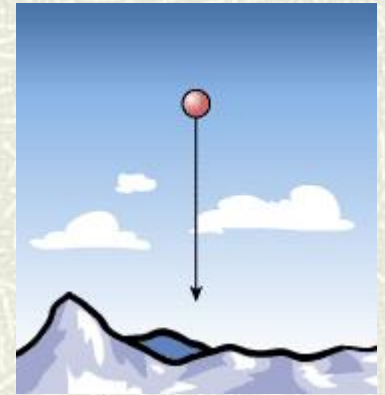
Evidence for special relativity

Invariance of the speed of light

Always measured as c

Time dilation

The long-lived muon



$$2 \mu s \rightarrow 22 \mu s$$

Particle experiments at the LHC

Maximum velocity = c

Mass increase

Particle creation $E = mc^2$



The general theory of relativity (1916)

General relativity

Relativity and accelerated motion?

Relativity and gravity?



The equivalence principle

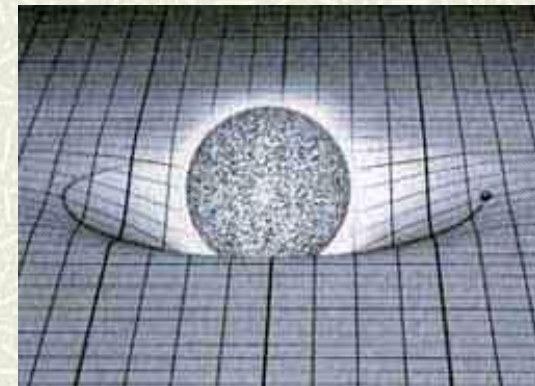
No distinction between inertial and gravitational mass

A new theory (1916)

Space-time distorted by mass

Gravity = curvature of space-time

$$G_{\mu\nu} = -\kappa T_{\mu\nu}$$



Evidence

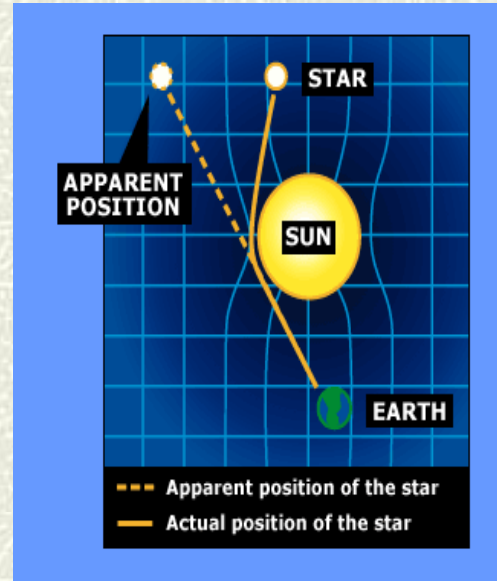
Orbit of Mercury

Bending of starlight by the sun (Eddington, 1919)

Evidence for general relativity

⌘ Bending of distant light by stars

Gravitational lensing



⌘ Gravitational time dilation

GPS corrections



⌘ Black holes

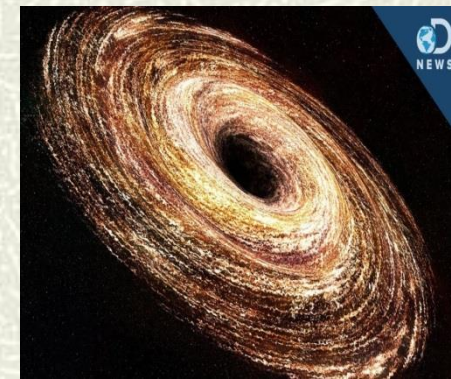
Centre of galaxies

$$G_{\mu\nu} = -\kappa T_{\mu\nu}$$

⌘ Gravitational waves

Hulse-Taylor (1979): energy loss in binary pulsar

LIGO (2016); gravitational waves



II Relativity and the universe

⌘ Apply general relativity to the cosmos (1917)

Ultimate test for new theory of gravity

⌘ Dynamic universe?

Expanding or contracting

$$G_{\mu\nu} = -\kappa T_{\mu\nu}$$

⌘ Static universe (observation)

Add new term to field equations

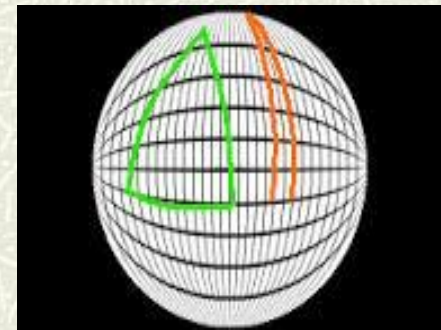
Cosmological constant λ

$$G_{\mu\nu} + \lambda g_{\mu\nu} = -\kappa T_{\mu\nu}$$

⌘ Bounded universe

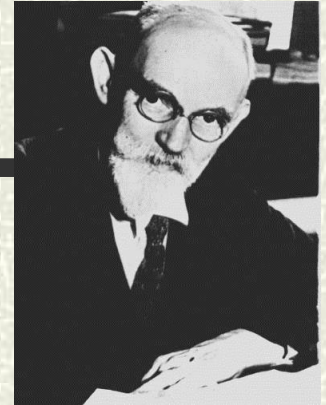
Cosmic radius and matter density defined by λ

No empty space at infinity (Mach's principle)



Static, bounded universe

De Sitter's universe (1917)



Alternative static solution

'Empty' universe

$$G_{\mu\nu} + \lambda g_{\mu\nu} = 0$$

Disliked by Einstein

Conflict with Mach's principle

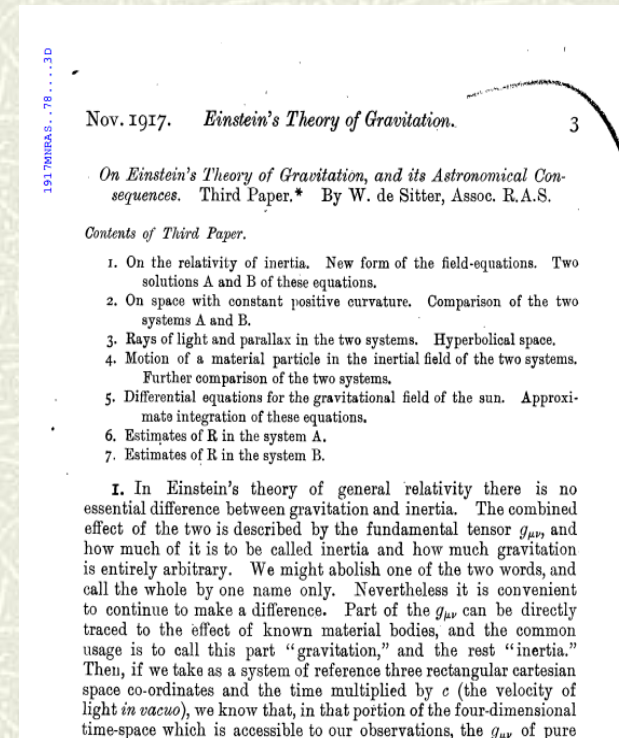
Beginning of Einstein's dislike for cosmic constant

Interest from astronomers

Prediction of redshifts – Slipher effect?

Confusion: static or non-static model?

Weyl 1923, Lanczos 1923, Lemaître 1925



Friedman's universe



*Alexander Friedman
(1888 -1925)*

▣ Allow time-varying solutions (1922)

Closed spatial curvature

$$G_{\mu\nu} + \lambda g_{\mu\nu} = -\kappa T_{\mu\nu}$$

▣ Expanding or contracting universe

▣ Badly received

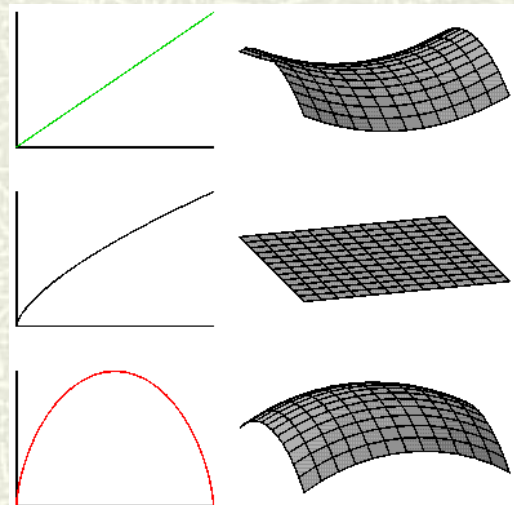
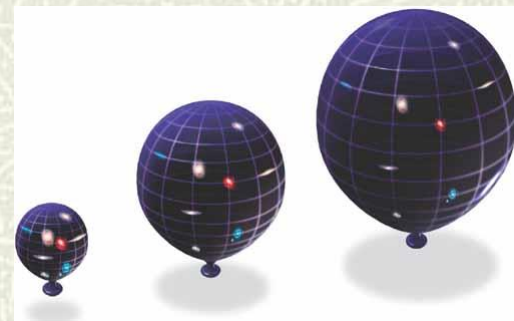
Considered “suspicious” by Einstein

“To this a physical reality can hardly be ascribed”

▣ Further Friedman models (1924)

Negative spatial curvature

Cosmic evolution, geometry depends on matter content



Lemaître's universe (1927)



Fr Georges Lemaître

Expanding model of the cosmos from GR

Compare with astronomy

Redshifts of the spiral nebulae (Slipher)

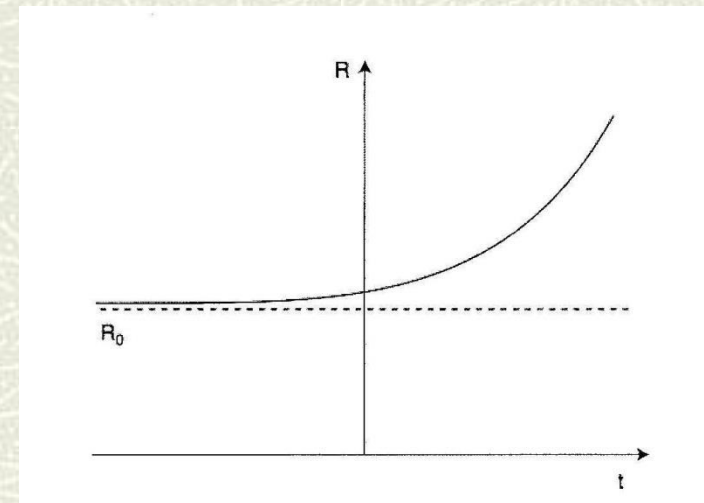
Distances of the spiral nebulae (Hubble)

Evidence of cosmic expansion?

Ignored by community

Belgian journal (in French)

Einstein: "Votre physique est abominable"



The watershed (1929)



Edwin Hubble (1889-1953)

- Spiral nebulae far beyond Milky Way

A universe of galaxies (1925)

- A linear relation between redshift and distance : Hubble's law (1929)

$$v = H_0 d \quad \text{with } H = 500 \text{ kms}^{-1} \text{Mpc}^{-1}$$

- Landmark result in astronomy

*Far-away galaxies rushing away
at a speed proportional to distance*

Velocity-Distance Relation among Extra-Galactic Nebulae.

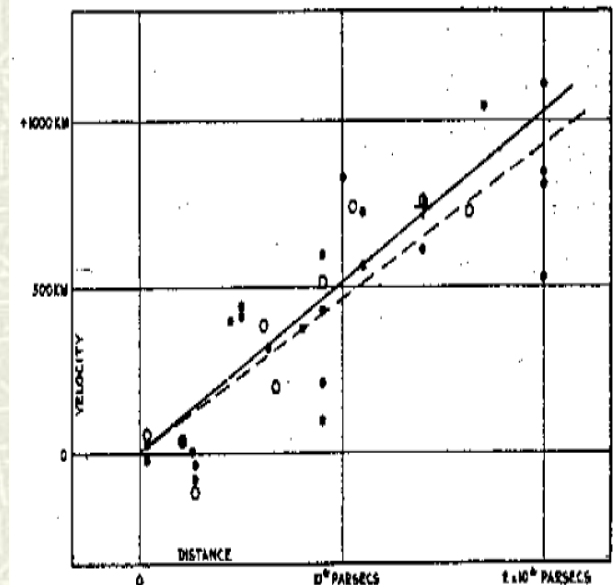


FIGURE 1

The expanding universe (1930)

- **RAS meeting (1930)**

*If redshifts are velocities, and if effect is non-local
Static cosmic models don't match observations*

- **Expanding universe?**

Hubble's law = expansion of space?

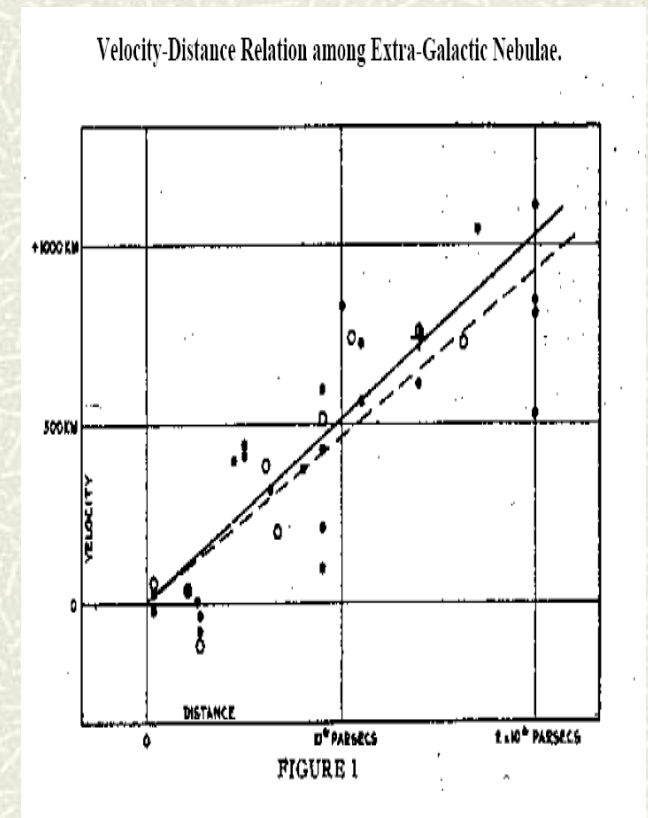
$$H = 500 \text{ kms}^{-1} \text{Mpc}^{-1}$$

- **Friedman-Lemaître model circulated**

Time-varying radius

Evolving models

Time-varying density of matter



Models of the expanding universe

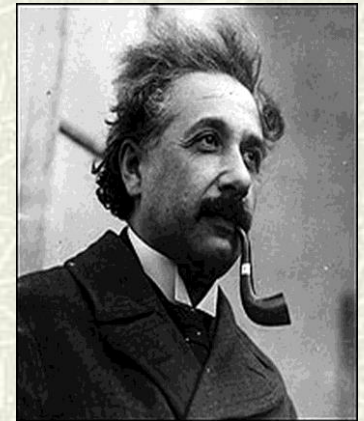
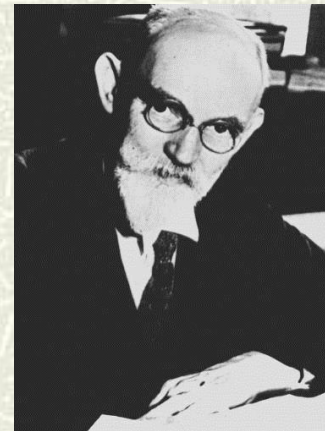
- **Eddington (1930, 31)**

*On the instability of the Einstein universe
Expansion caused by condensation?*



- **Tolman (1930, 31)**

*On the behaviour of non-static models
Expansion caused by annihilation of matter ?*



- **de Sitter (1930, 31)**

*Further remarks on the expanding universe
Expanding universes of every flavour*

- **Einstein (1931, 32)**

*Friedman-Einstein model $\lambda = 0, k = 1$
Einstein-de Sitter model $\lambda = 0, k = 0$*

New: also a steady –state model

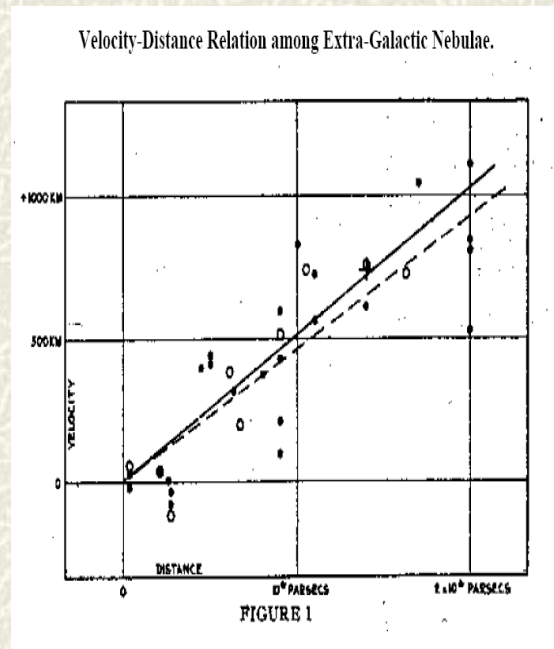
$$G_{\mu\nu} = -\kappa T_{\mu\nu}$$

The big bang model (1931)



Fr Georges Lemaître

- ✚ Expanding U smaller in the past
- ✚ Rewind to early epochs
- ✚ Extremely dense, extremely hot
- ✚ Explosive beginning at $R = 0$?
- ✚ Expanding and cooling ever since



Later called *'The big bang'*

A second line of evidence

How were the chemical elements formed?

In the stars? Why so much Hydrogen?

Elements formed in the hot big bang?

Georges Gamow

Predicts $U = 75\%$ Hydrogen, 25% Helium

Agreement with observation

Victory for big bang model

(Heavier atoms formed in stars)



Georges Gamow



A third line of evidence

■ Infant universe very hot indeed

Dominated by radiation

■ Still observable today?

A fossil from the early universe

■ The cosmic microwave background

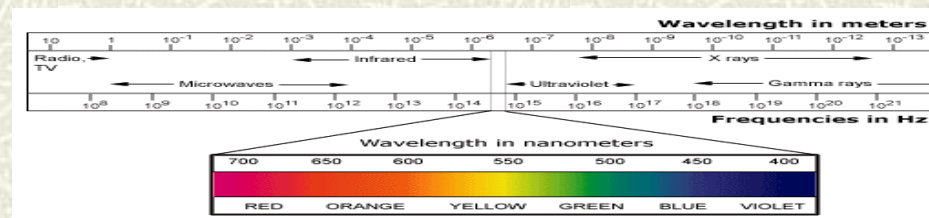
Low temp, microwave frequency

Released when atoms formed (300,000 yr)



Alpher, Gamow and Herman

No-one looked (1940s)



Steady-state universe (1948)

Alternative to big bang

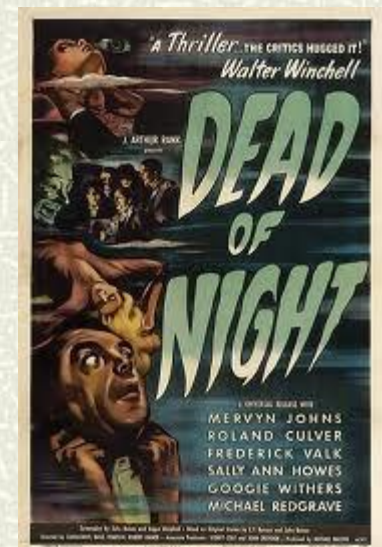
Hoyle, Bondi and Gold

Expanding, unchanging universe?

Continuous creation of matter

Very little matter needed

No assumptions about early epochs

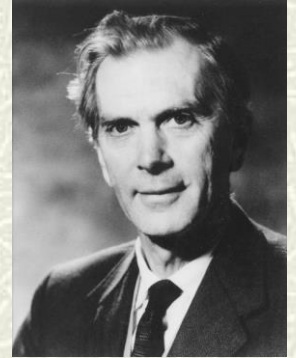


Steady-state vs big bang

✦ Radio-astronomy (1950s, 1960s)

Galaxy distributions at different epochs

Evidence of evolution



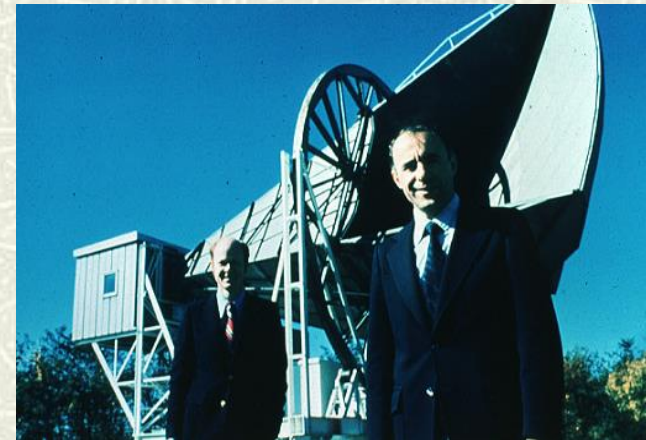
Martin Ryle

✦ Quasars, pulsars (1960s)

✦ Cosmic microwave background (1965)

Low temperature, low frequency

Remnant of young, hot universe

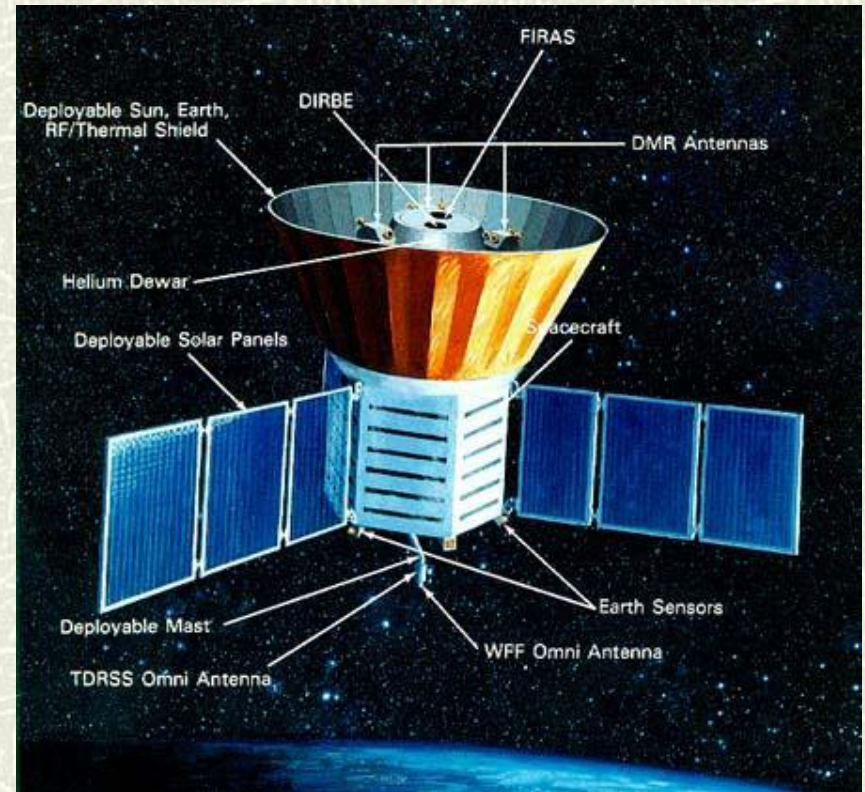


Penzias and Wilson (1965)

Strong support for big bang model

Modern measurements of the CMB

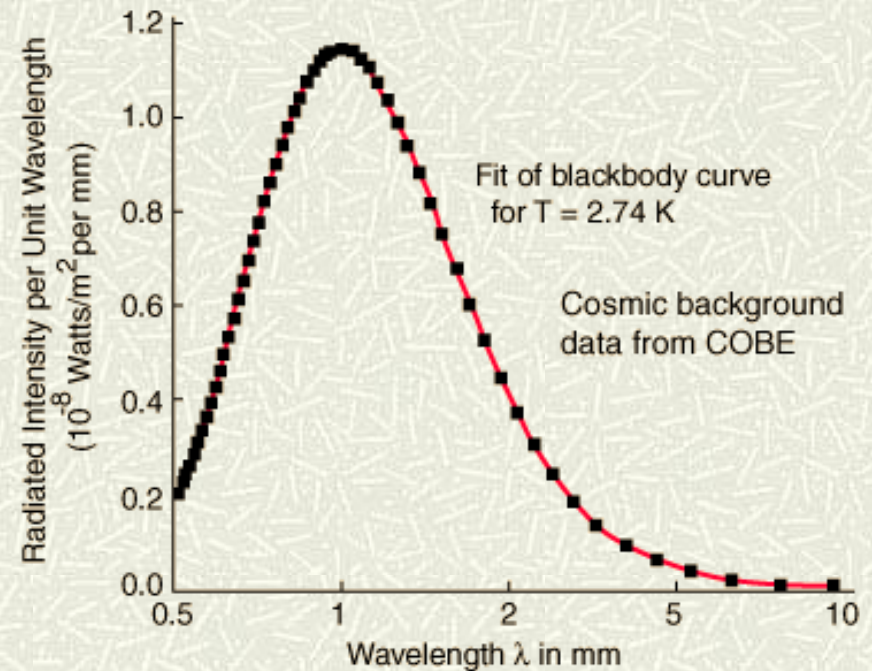
- Details of background radiation
 - Full spectrum
 - Comparison with theory
 - Perturbations?
-
- *Ground telescopes*
 - *Balloon experiments*
 - *Satellite experiments*



COBE satellite (1992)

COBE measurements of CMB

- Expected temperature
- Expected frequency
- Perfect blackbody spectrum
- *Radiation very uniform*
- *Variation of 1 in 10^5*
- *Seeds of galaxies ?*



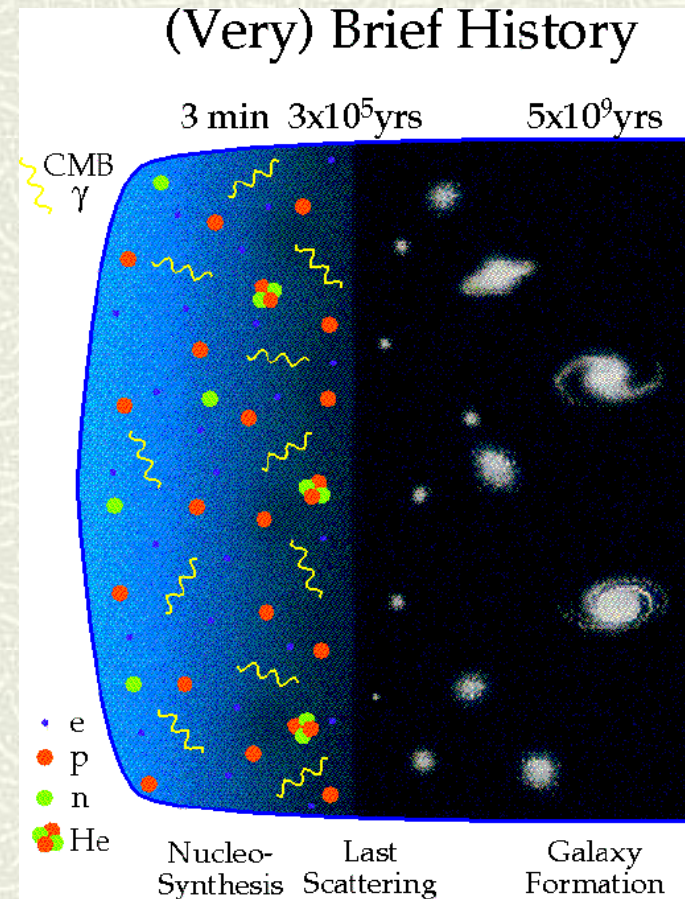
Nobel Prize

COBE (1992)

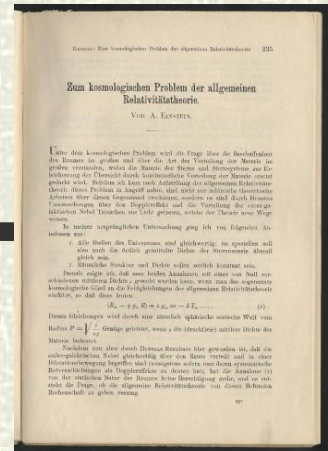
The big bang – evidence

1. The expansion of the U
2. The abundance of H and He
3. The distribution of the galaxies
4. The cosmic microwave background

How did it start?

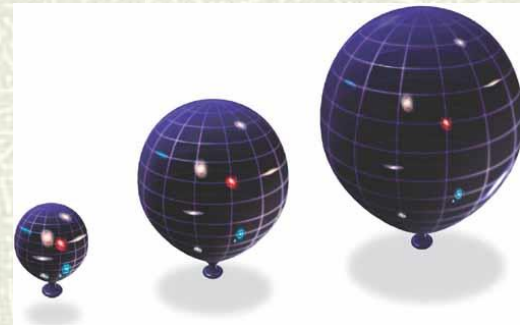


III Einstein's 1931 model



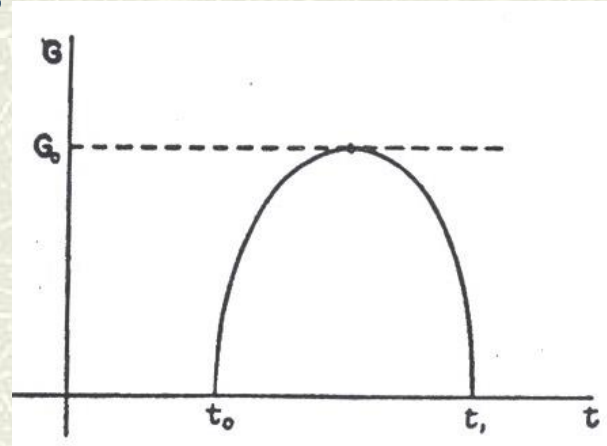
✚ **Einstein's first dynamic model of the cosmos**
Rarely cited (German)

✚ **Adopts Friedman 1922 model**
Time-varying, closed universe: $k = 1$
Cosmic constant redundant: set $\lambda = 0$



✚ **Use Hubble to extract empirical parameters**
Radius $R \sim 10^8$ lyr , timespan 10^{10} yr
Density of matter $\rho \sim 10^{-26}$ g/cm³

✚ **Not a cyclic model**



Einstein's 1931 model (research)

First translation into English

O'Raifeartaigh and McCann 2014

Anomalies in calculations

$R \sim 10^8 \text{ lyr} : \text{ should be } 10^9 \text{ lyr}$

$\rho \sim 10^{-26} \text{ g/cm}^3 : \text{ should be } 10^{-28} \text{ g/cm}^3$

$t \sim 10^{10} \text{ yr} : \text{ should be } 10^9 \text{ yr}$

Error in Hubble constant

Oxford blackboard: $D^2 \sim 10^{-53} \text{ cm}^{-2}$

Implications for timespan problem

$$D = \frac{1}{c} \frac{1}{l} \frac{dl}{dt} = \frac{1}{c} \frac{1}{P} \frac{dP}{dt}$$

$$D^2 = \frac{1}{P^2} \frac{P_0 - P}{P} \sim \frac{1}{P^2} \quad (1a)$$

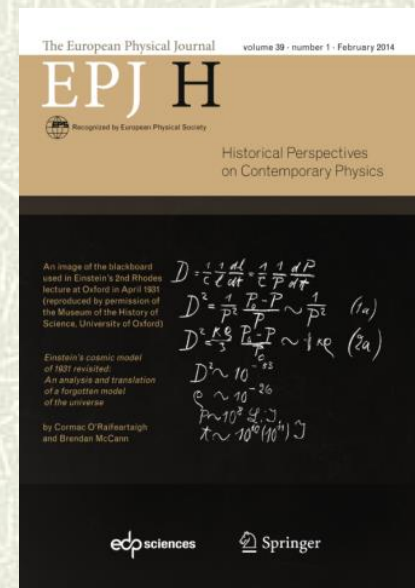
$$D^2 = \frac{K}{3} \frac{P_0 - P}{P} \sim \frac{1}{KP} \quad (2a)$$

$$D^2 \sim 10^{-53}$$

$$c \sim 10^{-26}$$

$$P \sim 10^8 \text{ g/cm}^3$$

$$t \sim 10^{10} (10^{11}) \text{ yr}$$



Finding 2: Einstein's steady-state model

Unpublished manuscript

Archived as draft of Einstein's 1931 model

Steady-state model

Expanding model of constant density

"The density is constant and determines the expansion"

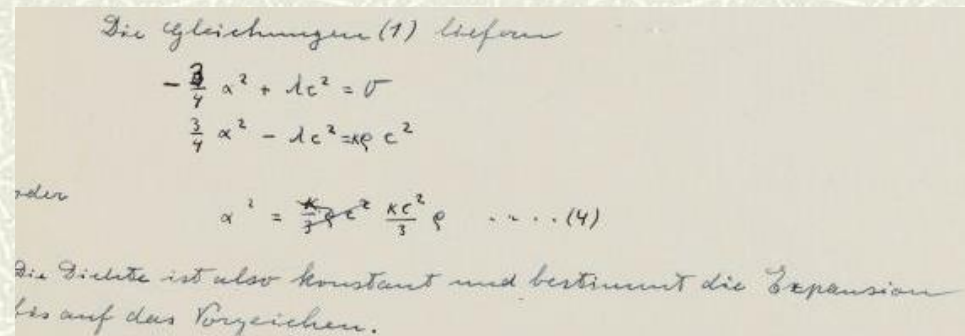
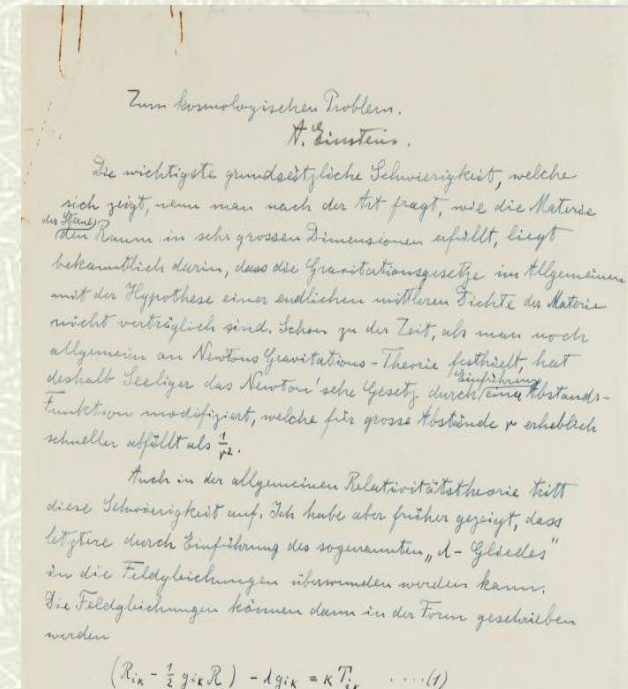
Continuous creation

Continuous formation of matter from vacuum

Associated with cosmic constant

Fatal flaw: abandoned

Evolving models adopted instead



Abandoned model

- ✦ **Correct geometry**
de Sitter line element

- ✦ **Simultaneous equations**
Error in derivation
Null solution

- ✦ **Einstein's crossroads**
Realised problem on revision
Declined to amend model

- ✦ **Evolving models**
Less contrived and set $\lambda = 0$

Im Nachfolgenden will ich auf eine Lösung der Gleichung (1) aufmerktsam machen, welche Hubble's Thatsachen gerecht wird, und in welcher die Dichte zeitlich konstant ist. Diese Lösung ist zwar in dem allgemeinen Schema Tolman's enthalten, scheint aber bisher nicht in Betracht gezogen worden zu sein.

1. Ich setze an

$$ds^2 = -e^{\alpha t} (dx_1^2 + dx_2^2 + dx_3^2) + c^2 dt^2 \dots (3)$$

Die Gleichungen (1) liefern

$$-\frac{3}{4} \alpha^2 + \lambda c^2 = 0$$
$$\frac{3}{4} \alpha^2 - \lambda c^2 = \kappa \rho c^2$$

oder

$$\alpha^2 = \frac{\kappa}{3} \rho c^2 \dots (4)$$

Die Dichte ist also konstant und bestimmt die Expansion bis auf das Vorzeichen.

Der Erhaltungssatz bleibt dadurch un verletzt, dass bei Setzung des λ -Gleides der Raum selbst nicht energetisch leer ist; seine Ueltung wird bekanntlich durch die Gleichungen (1) gewährleistet.

Einstein's lost theory uncovered

Physicist explored the idea of a steady-state Universe in 1931.

Daide Castelvechi

24 February 2014

New Discovery Reveals Einstein Tried To Devise A Steady State Model Of The Universe

2 comments, 2 called-out + Comment Now + Follow Comments

Almost 20 years before the late Fred Hoyle and his colleagues devised the [Steady State Theory](#), Albert Einstein toyed with a similar idea: that the universe was eternal, expanding outward with a consistent input of spontaneously generating matter.

An Irish physicist came across the paper last year and could hardly believe. According to this week's article in [Nature](#),

model of the universe very different to today's [Big Bang](#) Theory.

The manuscript, which hadn't been referred to by scientists for decades,



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Einstein's Lost Theory Uncovered

The famous physicist explored the idea of a steady-state universe in 1931

nature

Feb 25, 2014 | By Daide Castelvechi and Nature magazine

A manuscript that lay unnoticed by scientists for decades has revealed that Albert Einstein once dabbled with an



www.irishtimes.com/news/science/wit-researchers-discover-lost-einstein-model-of-universe-1.1713487

THE IRISH TIMES

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Monday, March 10, 2014

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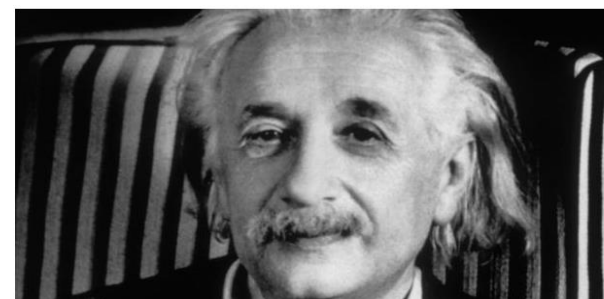
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WIT researchers discover 'lost' Einstein model of universe

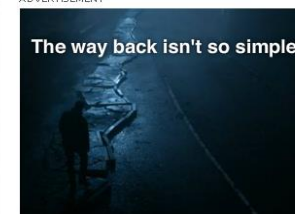
Scientists uncovered misfiled papers while searching Jerusalem university's online archive



Latest Ireland »

- 12:26 Quinn confirms Flannery approached him with Rehab concerns
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- 09:05 Family hope public appeal will help daughter beat cancer
- 08:42 Gardaí investigate death of woman in Dublin
- 08:25 Flannery faces call from all parties to attend PAC

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100 years of general relativity

Published May 1916

From Swiss patent office to Berlin

A new theory of gravity

Gravity = curvature of spacetime

Predictions supported by experiment

Bending of light by a star

Expanding universe

Gravitational time dilation (GPS)

One more test

Gravitational waves - LIGO 2016!



Einstein in Berlin (1918)

Einstein's universe: conclusions

Cosmology = test for general relativity

Introduces cosmic constant

Embraces dynamic cosmology

New evidence – new models

Steady-state model

Evolving models simpler: remove cosmic constant

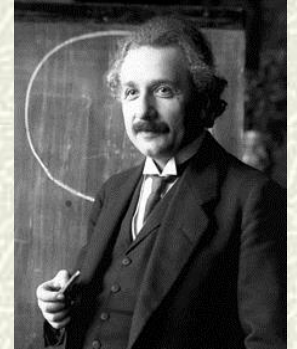
The evolving universe

Extract observational parameters

Timespan problem attributed to simplifying assumptions

No discussion of origins

Wary of extrapolations to early epochs



Hubble constant revised

Einstein Archives Online

Albert Einstein



Digitized Manuscripts



Finding Aid



Archival Database



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Albert Einstein Archives
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JPG

Über das sogenannte kosmologische Problem.

by Einstein, Albert (Author)

Date: 1932-09-01

Archival Call Number: 1-115

Document Type: Autograph Draft of Document (ADDf)



DB Info

Kosmologische Betrachtungen zur allgemeinen Relativitätstheorie.

by Einstein, Albert (Author)

Date: 1917-02-08

Archival Call Number: 90-9

Document Type: Printed Document (PD)



DB Info

Die Beantwortung Ihrer Frage, überhaupt kosmologischer Fragen

by Einstein, Albert (Author)

Date: 1929-09-20

Archival Call Number: 25-231

Document Type: Carbon/File Copy of Typed Letter (TLC)



DB Info

Das kosmologische Glied soll überholt sein.

by Hopf, Ludwig (Author)

Date: 1932-06-14

Archival Call Number: 13-306

Document Type: Autograph Letter Signed (ALS)

Einstein Archives Online

Albert Einstein

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Über das sogenannte kosmologische Problem.

Archival Call Number: 1-115

Begin Date: 1932-09-01

End Date: 1932-09-30

Main Author: Einstein, Albert (Author)

Other Persons: Mayer, Walther (Author)

Language: German

Archival Location: Albert Einstein Archives, The Hebrew University of Jerusalem, Israel

Number of Pages: 11.



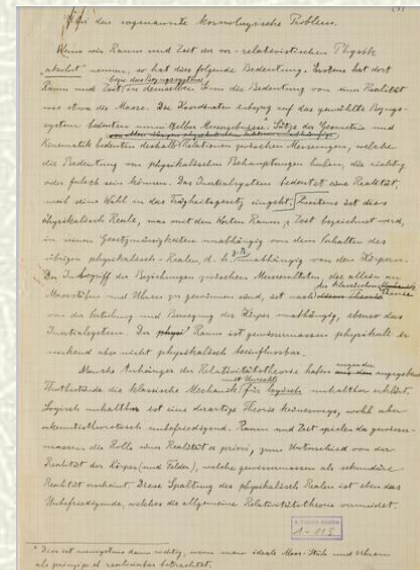
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Einstein's steady-state model and cosmology today

Dark energy (1998)

Accelerated expansion (observation)

Positive cosmological constant

Einstein's dark energy

“The conservation law is preserved in that, by setting the λ -term, space itself is not empty of energy; its validity is well known to be guaranteed by equations (1).”

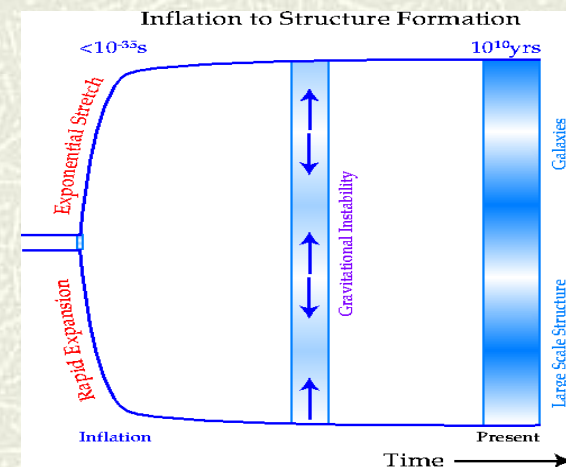
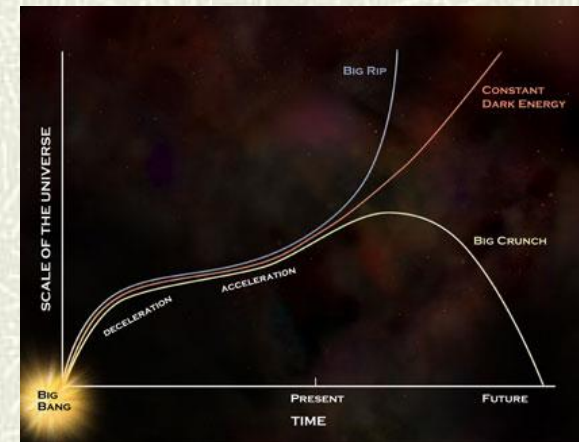
Cosmic inflation

Inflationary models use de Sitter metric

Used in all steady-state models

Flat curvature, constant rate of matter creation

Different time-frame!



Einstein's steady-state model: key quotes

New solution

“In what follows, I wish to draw attention to a solution to equation (1) that can account for Hubbel’s facts, and in which the density is constant over time”

Matter creation

“If one considers a physically bounded volume, particles of matter will be continually leaving it. For the density to remain constant, new particles of matter must be continually formed within that volume from space “

Dark energy

“The conservation law is preserved in that, by setting the λ -term, space itself is not empty of energy; its validity is well known to be guaranteed by equations (1).”

Einstein-de Sitter model (1932)

✚ Curvature not a given in dynamic models

Not observed empirically

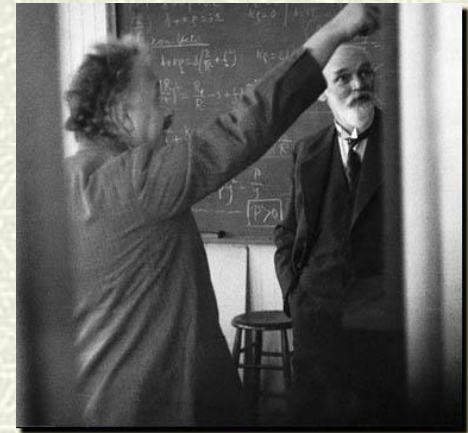
Remove spatial curvature (Occam's razor)

$$ds^2 = -R^2(dx^2 + dy^2 + dz^2) + c^2 dt^2$$

$$\frac{3R'^2}{R^2} + \frac{3c^2}{R^2} - \lambda = \kappa c^2 \rho,$$

$$\frac{1}{R^2} \left(\frac{dR}{cdt} \right)^2 = \frac{1}{3} \kappa \rho.$$

$$h^2 = \frac{1}{3} \kappa \rho$$



✚ Simplest Friedman model

Time-varying universe with $\lambda = 0$, $k = 0$

Important hypothetical case: critical universe

Critical density : $\rho = 10^{-28} \text{ g/cm}^3$

✚ Becomes standard model

Despite high density of matter

Despite age problem

Time evolution not considered in paper – see title

PROCEEDINGS OF THE NATIONAL ACADEMY OF SCIENCES

Volume 18

March 15, 1932

Number 3

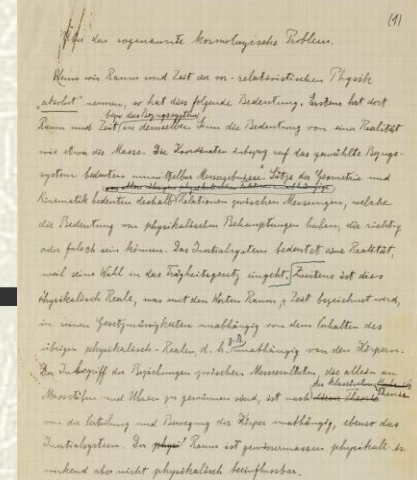
ON THE RELATION BETWEEN THE EXPANSION AND THE MEAN DENSITY OF THE UNIVERSE

BY A. EINSTEIN AND W. DE SITTER

Communicated by the Mount Wilson Observatory, January 25, 1932

In a recent note in the *Göttinger Nachrichten*, Dr. O. Heckmann has pointed out that the non-static solutions of the field equations of the general theory of relativity with constant density do not necessarily imply a positive curvature of three-dimensional space, but that this curvature may also be negative or zero.

Einstein-de Sitter model revisited



■ Einstein's cosmology review of 1933

Review of dynamic models from first principles

Culminates in Einstein-de Sitter model

Cosmic constant banished

Possibility of flat geometry

$$2A \frac{d^2 A}{dt^2} + \left(\frac{dA}{dt} \right)^2 = 0$$

$$3 \left(\frac{\frac{dA}{dt}}{A} \right)^2 = \kappa \rho c^2.$$

■ Parameters extracted

Critical density of 10^{-28} g/cm³ : reasonable

Timespan of 10^{10} years: conflict with astrophysics

Attributed to simplifications (incorrect estimate)

$$3h^2 = \kappa \rho c^2 (= 8\pi K \rho)$$

$$A = c(t - t_0)^{\frac{2}{3}}$$



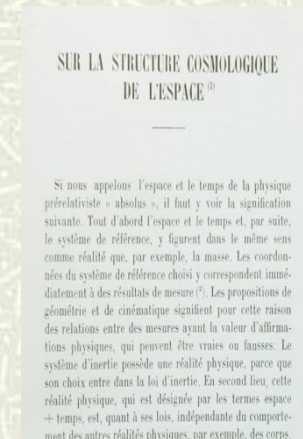
■ Published in 1933!

French book; small print run

Intended for scientific journal; not submitted

Significant paper

$$t - t_0 = \frac{2}{3h}$$



Einstein's steady-state theory: a significant find?

✦ New perspective on steady-state theory (1950s)

Logical possibility: not a crank theory

✦ Insight into scientific progress

Evolution of successful theories

No Kuhnian paradigm shift to 'big bang' model

Slow dawning

✦ Insight into Einstein's philosophy

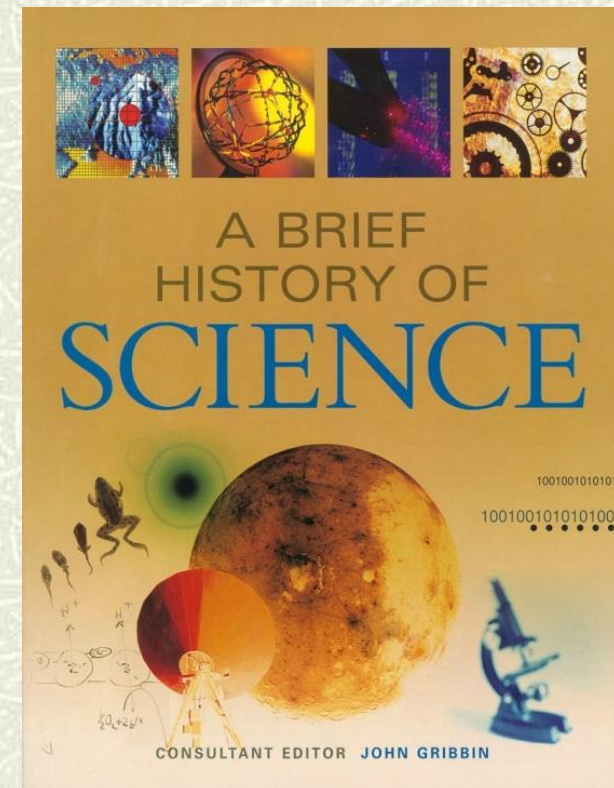
Simple solution?

Discards model rather than introduce new term to GFE

Occam's razor approach

✦ Links with modern cosmology

Dark energy, cosmic inflation



*Paradigm shift or
slow dawning ?*

Explanation for runaway galaxies?

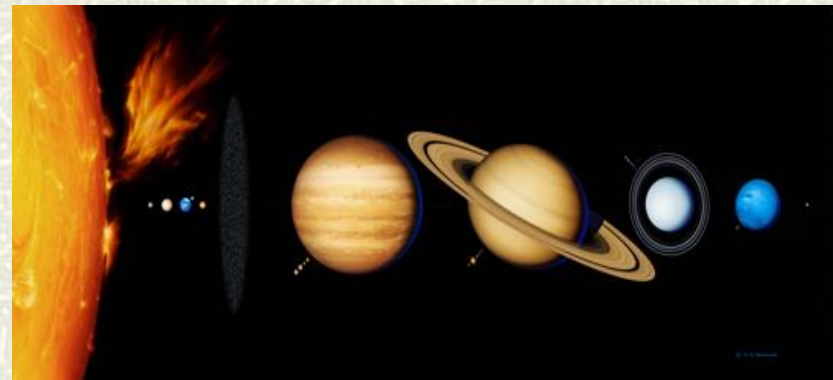
Newton

- Gravity pulls in not out
- Space is fixed
- Time has no beginning



Isaac Newton

*How can galaxies be receding?
What is pushing out?*



Results: publications

■ Einstein's 1931 model

Einstein's cosmic model of 1931 revisited; an analysis and translation of a forgotten model of the universe. O'Raifeartaigh, C. and B. McCann. 2014 **Eur. Phys. J (H)** 39(1):63-85

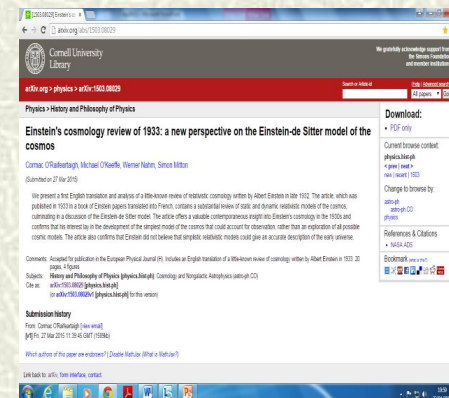
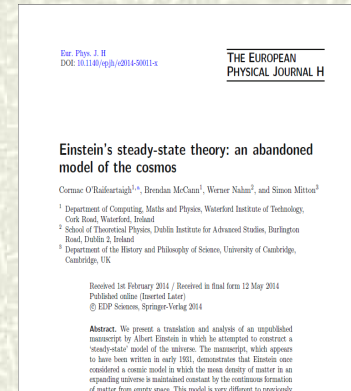
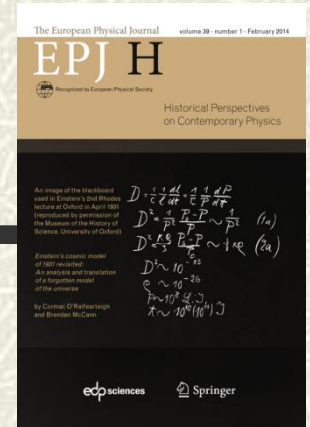
■ Einstein's steady-state manuscript

Einstein's steady-state theory: an abandoned model of the cosmos. O'Raifeartaigh, C., B. McCann, W. Nahm and S. Mitton. 2014 **Eur. Phys. J (H)** 39(3):353-367

■ Einstein-de Sitter model

Einstein's cosmology review of 1933: a new perspective on the Einstein-de Sitter model of the cosmos. O'Raifeartaigh, C., M.O'Keeffe, W. Nahm and S. Mitton. 2015. To be published in **Eur. Phys. J (H)**

■ Review paper: conclusions



ORIGINS OF THE EXPANDING UNIVERSE:
1912–1932



Edited by
Michael J. Way and Deidre Hunter

Einstein's steady-state theory: an abandoned model of the cosmos

Cormac O'Riartaigh^{1,a}, Brendan McCann¹, Werner Nahm², and Simon Mitton³

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Abstract. We present a translation and analysis of an unpublished manuscript by Albert Einstein in which he attempted to construct a 'steady-state' model of the universe. The manuscript, which appears to have been written in early 1931, demonstrates that Einstein once considered a cosmic model in which the mean density of matter in an expanding universe is maintained constant by the continuous formation of matter from empty space. This model is very different to previously

Einstein's cosmic model of 1931 revisited: an analysis and translation of a forgotten model of the universe

C. O'Riartaigh^a and B. McCann

Department of Computing, Maths and Physics, Waterford Institute of Technology, Cork Road, Waterford, Ireland

Received 21 September 2013 / Received in final form 20 December 2013
Published online 4 February 2014
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Abstract. We present an analysis and translation of Einstein's 1931 paper "Zum kosmologischen Problem der allgemeinen Relativitätstheorie" or "On the cosmological problem of the general theory of relativity". In this little-known paper, Einstein proposes a cosmic model in which the universe undergoes an expansion followed by a contraction, quite different to the monotonically expanding Einstein-de Sitter model of 1932. The paper offers many insights into Einstein's cosmology in the light of the first evidence for an expanding universe and we consider his views of issues such as the curvature of space, the cosmological constant, the singularity and the timespan of the expansion. A number of original

An image of the blackboard used in Einstein's 2nd Rhodes lecture at Oxford in April 1931 (reproduced by permission of the Museum of the History of Science, University of Oxford)

$$\begin{aligned} D &= \frac{1}{c} \frac{d}{dt} = \frac{1}{c} \frac{d}{P} \frac{dP}{dt} \\ D^2 &= \frac{1}{P^2} \frac{d^2 P}{dt^2} \sim \frac{1}{P^2} \quad (1a) \\ D^2 &= \frac{K}{3} \frac{P_0 - P}{P} \sim \frac{1}{P} \quad (2a) \\ D^2 &\sim 10^{-53} \\ c &\sim 10^{-26} \\ P &\sim 10^8 \text{ yr} \\ \tau &\sim 10^{10} (10^{11}) \text{ yr} \end{aligned}$$

Einstein's cosmic model of 1931 revisited: An analysis and translation of a forgotten model of the universe

by Cormac O'Riartaigh and Brendan McCann

arXiv.org > physics > arXiv:1303.08029

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Comments: Accepted for publication in the European Physical Journal (H). Includes an English translation of a little-known review of cosmology written by Albert Einstein in 1933. 20 pages, 4 figures

Subjects: History and Philosophy of Physics (physics.hist-ph); Cosmology and Nongalactic Astrophysics (astro-ph.CO)

Cite as: arXiv:1303.08029 [physics.hist-ph] (or arXiv:1303.08029v1 [physics.hist-ph] for this version)

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From: Cormac O'Riartaigh [view email]
[v1] Fri, 27 Mar 2014 11:38:45 GMT (1594k)

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• NASA ADS

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Comments: 20 pages, 2 figures. To be published in the book 'The Philosophy of Cosmology: Foundations and Perspectives' (Cambridge University Press)

Subjects: History and Philosophy of Physics (physics.hist-ph); Cosmology and Nongalactic Astrophysics (astro-ph.CO)

Cite as: arXiv:1304.02873 [physics.hist-ph] (or arXiv:1304.02873v1 [physics.hist-ph] for this version)

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From: Cormac O'Riartaigh [view email]
[v1] Sat, 11 Apr 2014 13:38:45 GMT (633k)

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Die Gleichungen (1) liefern

$$-\frac{3}{4}\alpha^2 + \lambda c^2 = 0$$

$$\frac{3}{4}\alpha^2 - \lambda c^2 = \kappa \rho c^2$$

oder

$$\alpha^2 = \frac{\kappa c^2}{3} \rho c^2 \dots (4)$$

Die Dichte ist also konstant und bestimmt die Expansion bis auf das Vorzeichen.

Taking $T_{44} = \rho c^2$ (all other components zero) in the *time* component of equation (1) we obtain $\left(R_{44} - \frac{1}{2}g_{44}R\right) - \lambda g_{44} = \kappa \rho c^2$.

This gives on analysis $-3\alpha^2/4 + 3\alpha^2/2 - \lambda c^2 = \kappa \rho c^2$ the second of Einstein's simultaneous equations.

From the *spatial* component of equation (1), we obtain $\left(R_{ii} - \frac{1}{2}g_{ii}R\right) - \lambda g_{ii} = 0$.

This gives on analysis $3\alpha^2/4 - 3\alpha^2/2 + \lambda c^2 = 0$ for the first of the simultaneous equations.

It is plausible that Einstein made a sign error here, initially getting $3\alpha^2/4 + 3\alpha^2/2 + \lambda c^2 = 0$ for this equation. (W. Nahm)

Einstein's steady-state model and cosmology today

■ Accelerated expansion (1998)

Supernova measurements

Dark energy – positive cosmological constant



■ Einstein's dark energy

“The conservation law is preserved in that, by setting the λ -term, space itself is not empty of energy; its validity is well known to be guaranteed by equations (1).”

Anticipates positive cosmological constant

■ De Sitter line element

$$ds^2 = -e^{\alpha t} (dx_1^2 + dx_2^2 + dx_3^2) + c^2 dt^2 \dots$$

Necessary for all steady-state models

Identical to inflationary models (different time-frame)

The steady-state universe (1948)

‡ Expanding but unchanging universe

Hoyle, Bondi and Gold (1948)

Disliked speculation about physics of early epochs

Perfect cosmological principle?



Bondi, Gold and Hoyle

‡ Continuous creation of matter

Very little matter required

No beginning, no age paradox

‡ Replace λ with creation term (Hoyle)

$$G_{\mu\nu} + C_{\mu\nu} = -k T_{\mu\nu}$$

‡ Improved version (1962)

$$G_{\mu\nu} + \lambda g_{\mu\nu} = k T (C_{\mu} + C_{\nu})$$



Hoyle and Narlikar (1962)

Conclusions

Cosmology – a testing ground for general relativity?

Assumptions; space-time = space + time

Homogeneity and isotropy

Static universe



Dynamic cosmology

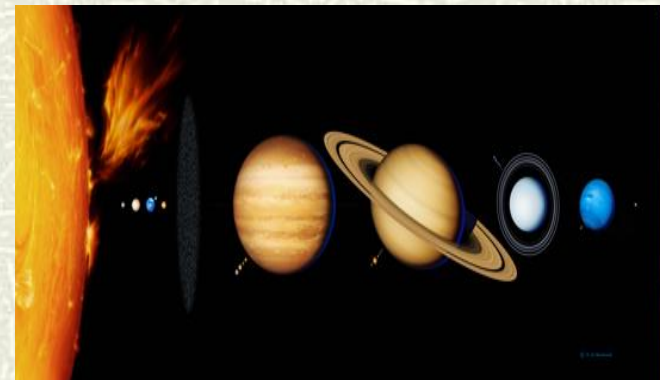
Steady-state universe?

Evolving models less contrived

Evolving models

Timespan problem: attributed to assumptions

Origins puzzle: ignored



Verdict

More data needed

III Astronomy and the Universe

The Great Debate (1900-1925)

Spiral nebulae = galaxies beyond Milky Way?

The Hooker telescope (1917)

Edwin Hubble (1921)

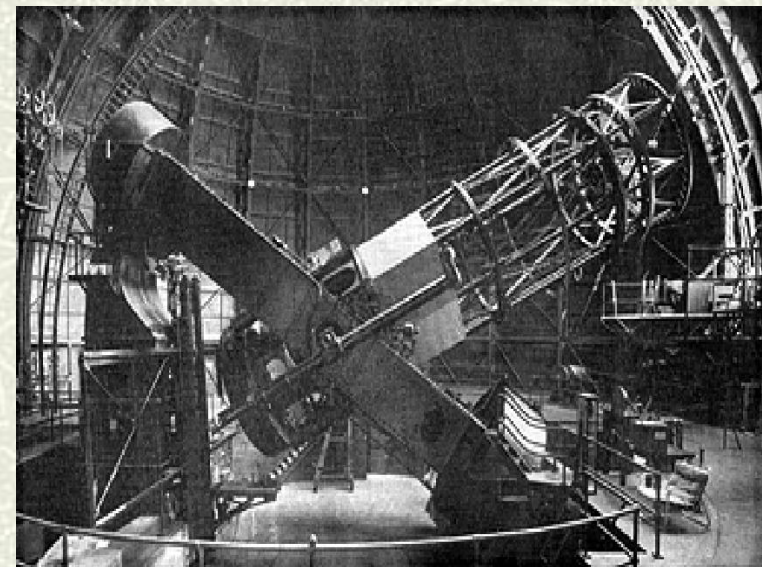
The distances of the nebulae (1925)

Cepheid variables resolved in two nebulae

Leavitt's period-luminosity relation

Spirals far beyond Milky Way

A universe of galaxies



The motion of the nebulae

The redshift of the nebulae

V.M Slipher (Lowell Observatory)

Light from most nebulae redshifted (1915, 1917)



Vesto Slipher

Doppler effect

*Frequency of light depends on
motion of source relative to observer*

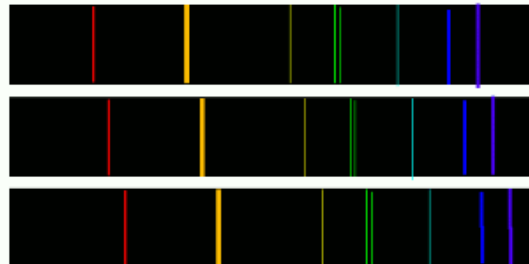
Nebulae moving outward?

Galaxies moving outward?

red shift

no motion

blue shift



Lowell Observatory

Cosmic background radiation

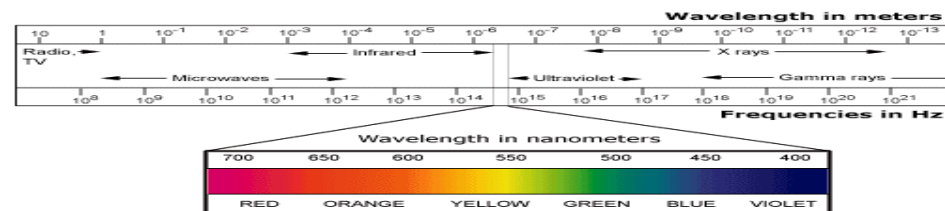
CMB discovered accidentally

- # Universal signal (1965)
- # Low frequency (microwave)
- # Low temperature (3K)

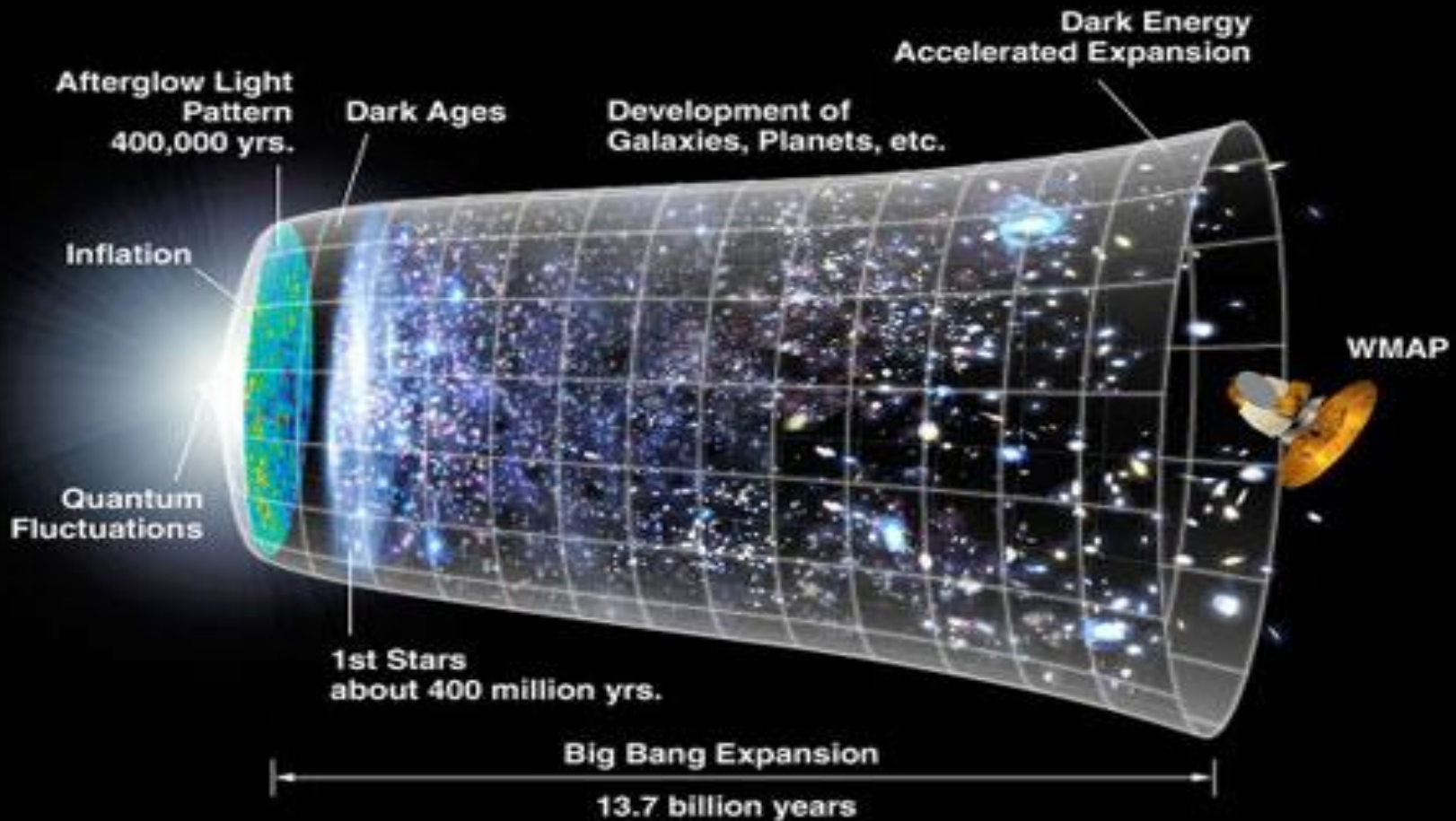


Penzias and Wilson (1965)

*Echo of **Big Bang!***



The big bang model



Overview

100 years of relativity

The special theory of relativity (1905)

The general theory of relativity (1916)

General relativity and the universe

The expanding universe (astronomy)

The big bang model

Einstein's universe

Some new discoveries

